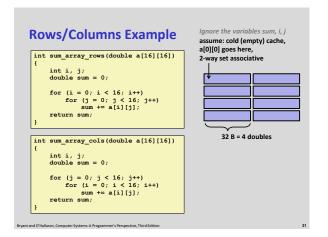
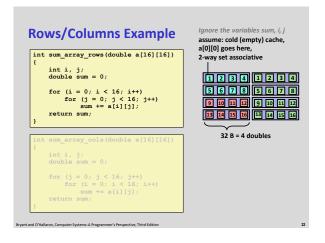
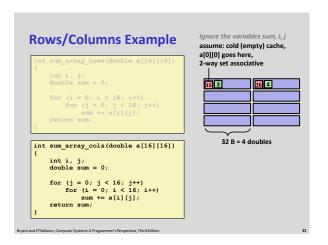


#### Let's think about those numbers Huge difference between a hit and a miss Could be 100x, if just L1 and main memory Would you believe 99% hits is twice as good as 97%? Consider: cache hit time of 1 cycle miss penalty of 100 cycles Average access time: 97% hits: 1 cycle + 0.03 \* 100 cycles = 4 cycles 99% hits: 1 cycle + 0.01 \* 100 cycles = 2 cycles This is why "miss rate" is used instead of "hit rate"

#### Writing Cache Friendly Code Make the common case go fast Focus on the inner loops of the core functions Minimize the misses in the inner loops Repeated references to variables are good (temporal locality) Stride-1 reference patterns are good (spatial locality) Key idea: Our qualitative notion of locality is quantified through our understanding of cache memories

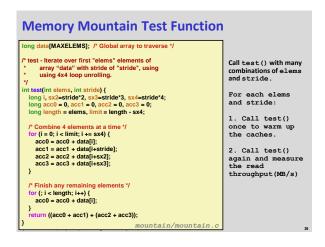


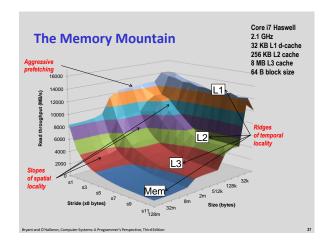




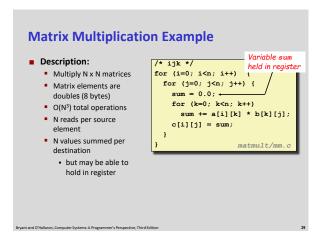


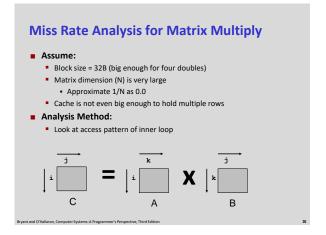
# The Memory Mountain Read throughput (read bandwidth) Number of bytes read from memory per second (MB/s) Memory mountain: Measured read throughput as a function of spatial and temporal locality. Compact way to characterize memory system performance.



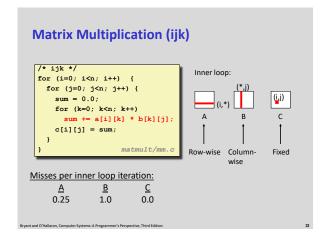


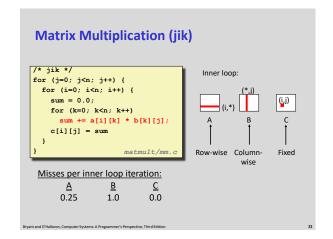


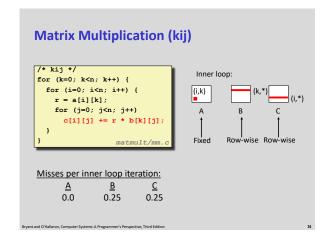


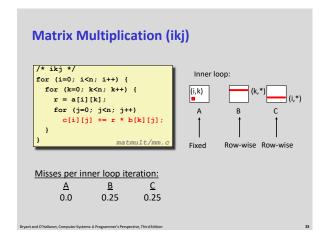


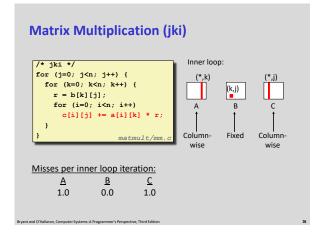
## Layout of C Arrays in Memory (review) C arrays allocated in row-major order each row in contiguous memory locations Stepping through columns in one row: for (i = 0; i < N; i++) sum += a[0][i]; accesses successive elements if block size (B) > sizeof(a<sub>ij</sub>) bytes, exploit spatial locality inis rate = sizeof(a<sub>ij</sub>) / B Stepping through rows in one column: for (i = 0; i < n; i++) sum += a[i][0]; accesses distant elements no spatial locality! miss rate = 1 (i.e. 100%)

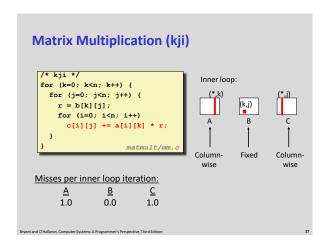


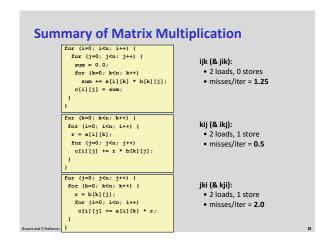


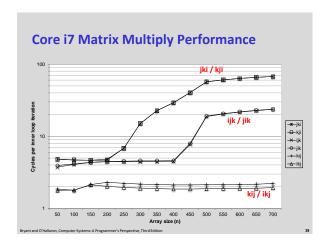


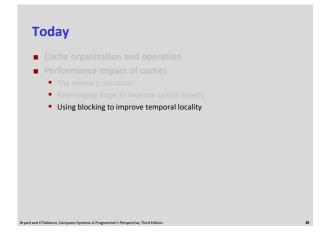


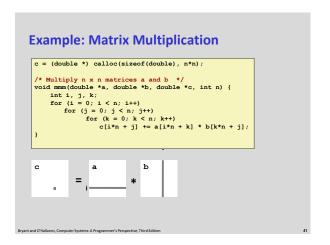


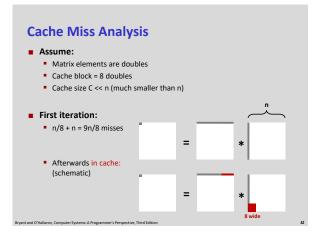




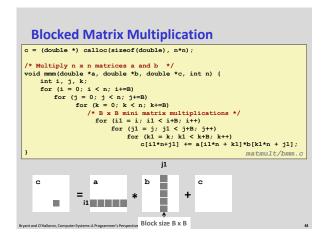


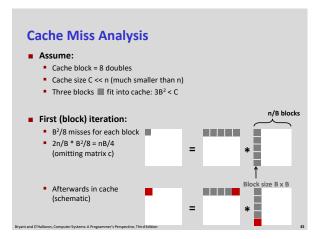


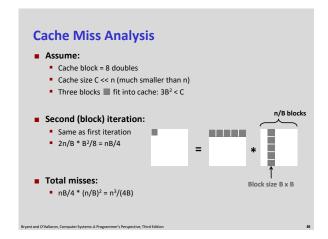




# Cache Miss Analysis Assume: Matrix elements are doubles Cache block = 8 doubles Cache size C << n (much smaller than n) Second iteration: Again: n/8 + n = 9n/8 misses Total misses: 9n/8 \* n² = (9/8) \* n³







## Blocking Summary No blocking: (9/8) \* n³ Blocking: 1/(4B) \* n³ Suggest largest possible block size B, but limit 3B² < C! Reason for dramatic difference: Matrix multiplication has inherent temporal locality: Input data: 3n², computation 2n³ Every array elements used O(n) times! But program has to be written properly

# Cache Summary Cache memories can have significant performance impact You can write your programs to exploit this! Focus on the inner loops, where bulk of computations and memory accesses occur. Try to maximize spatial locality by reading data objects with sequentially with stride 1. Try to maximize temporal locality by using a data object as often as possible once it's read from memory.