Program Optimization

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Today

- **Overview**
- **Generally Useful Optimizations**
  - Code motion/precomputation
  - Strength reduction
  - Sharing of common subexpressions
  - Removing unnecessary procedure calls
- **Optimization Blockers**
  - Procedure calls
  - Memory aliasing
- **Exploiting Instruction-Level Parallelism**
- **Dealing with Conditionals**

Performance Realities

There's more to performance than asymptotic complexity

- **Constant factors matter too!**
  - Easily see 10:1 performance range depending on how code is written
  - Must optimize at multiple levels:
    - algorithm, data representations, procedures, and loops
- **Must understand system to optimize performance**
  - How programs are compiled and executed
  - How modern processors + memory systems operate
  - How to measure program performance and identify bottlenecks
  - How to improve performance without destroying code modularity and generality

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Optimizing Compilers

- **Provide efficient mapping of program to machine**
  - register allocation
  - code selection and ordering (scheduling)
  - dead code elimination
  - eliminating minor inefficiencies
- **Don't (usually) improve asymptotic efficiency**
  - up to programmer to select best overall algorithm
  - big-O savings are (often) more important than constant factors
    - but constant factors also matter
- **Have difficulty overcoming "optimization blockers"**
  - potential memory aliasing
  - potential procedure side-effects

Limitations of Optimizing Compilers

- **Operate under fundamental constraint**
  - Must not cause any change in program behavior
    - Except, possibly when program making use of nonstandard language features
  - Often prevents it from making optimizations that would only affect behavior under pathological conditions.
- **Behavior that may be obvious to the programmer can be obfuscated by languages and coding styles**
  - e.g., Data ranges may be more limited than variable types suggest
- **Most analysis is performed only within procedures**
  - Whole-program analysis is too expensive in most cases
  - Newer versions of GCC do interprocedural analysis within individual files
    - But, not between code in different files
- **Most analysis is based only on *static* information**
  - Compiler has difficulty anticipating run-time inputs
- **When in doubt, the compiler must be conservative**

Generally Useful Optimizations

- **Optimizations that you or the compiler should do regardless of processor / compiler**

- **Code Motion**
  - Reduce frequency with which computation performed
    - If it will always produce same result
    - Especially moving code out of loop

```
void set_row(double *a, double *b,
   long i, long n)
{
    long j;
    for (j = 0; j < n; j++)
         a[n*i+j] = b[j];
}
```

→

```
    long j;
    int ni = n*i;
    for (j = 0; j < n; j++)
         a[ni+j] = b[j];
```

Compiler-Generated Code Motion (-O1)

```
void set_row(double *a, double *b,
   long i, long n)
{
    long j;
    for (j = 0; j < n; j++)
         a[n*i+j] = b[j];
}
```

```
    long j;
    long ni = n*i;
    double *rowp = a+ni;
    for (j = 0; j < n; j++)
         *rowp++ = b[j];
```

```
set_row:
        testq   %rcx, %rcx              # Test n
        jle     .L1                     # If 0, goto done
        imulq   %rcx, %rdx              # ni = n*i
        leaq    (%rdi,%rdx,8), %rdx     # rowp = A + ni*8
        movl    $0, %eax                # j = 0
.L3:                                    # loop:
        movsd   (%rsi,%rax,8), %xmm0    # t = b[j]
        movsd   %xmm0, (%rdx,%rax,8)    # M[A+ni*8 + j*8] = t
        addq    $1, %rax                # j++
        cmpq    %rcx, %rax              # j:n
        jne     .L3                     # if !=, goto loop
.L1:                                    # done:
        rep ; ret
```

Reduction in Strength

- Replace costly operation with simpler one
- Shift, add instead of multiply or divide

  `16*x   -->   x << 4`

  - Utility machine dependent
  - Depends on cost of multiply or divide instruction
    - On Intel Nehalem, integer multiply requires 3 CPU cycles
- Most valuable when it can be done within a loop
  - "Induction variable" has value linear in loop execution count

```
for (i = 0; i < n; i++) {
  int ni = n*i;
  for (j = 0; j < n; j++)
    a[ni + j] = b[j];
}
```

→

```
int ni = 0;
for (i = 0; i < n; i++) {
  for (j = 0; j < n; j++)
    a[ni + j] = b[j];
  ni += n;
}
```

Share Common Subexpressions

- Reuse portions of expressions
- GCC will do this with –O1

```
/* Sum neighbors of i,j */
up =    val[(i-1)*n + j  ];
down =  val[(i+1)*n + j  ];
left =  val[i*n     + j-1];
right = val[i*n     + j+1];
sum = up + down + left + right;
```

```
long inj = i*n + j;
up =    val[inj - n];
down =  val[inj + n];
left =  val[inj - 1];
right = val[inj + 1];
sum = up + down + left + right;
```

3 multiplications: i*n, (i–1)*n, (i+1)*n

1 multiplication: i*n

```
leaq   1(%rsi), %rax  # i+1
leaq   -1(%rsi), %r8  # i-1
imulq  %rcx, %rsi     # i*n
imulq  %rcx, %rax     # (i+1)*n
imulq  %rcx, %r8      # (i-1)*n
addq   %rdx, %rsi     # i*n+j
addq   %rdx, %rax     # (i+1)*n+j
addq   %rdx, %r8      # (i-1)*n+j
```

```
imulq    %rcx, %rsi   # i*n
addq     %rdx, %rsi   # i*n+j
movq     %rsi, %rax   # i*n+j
subq     %rcx, %rax   # i*n+j-n
leaq     (%rsi,%rcx), %rcx # i*n+j+n
```

Optimization Blocker #1: Procedure Calls

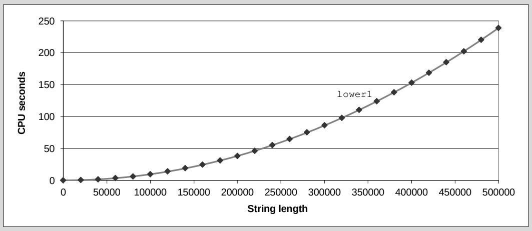
- **Procedure to Convert String to Lower Case**

```
void lower(char *s)
{
  size_t i;
  for (i = 0; i < strlen(s); i++)
    if (s[i] >= 'A' && s[i] <= 'Z')
      s[i] -= ('A' - 'a');
}
```

- Extracted from CMU 213 lab submissions, Fall, 1998
- Similar pattern seen in UMN HA1

Lower Case Conversion Performance

- Time quadruples when double string length
- Quadratic performance



Convert Loop To Goto Form

```
void lower(char *s)
{
   size_t i = 0;
   if (i >= strlen(s))
     goto done;
 loop:
   if (s[i] >= 'A' && s[i] <= 'Z')
       s[i] -= ('A' - 'a');
   i++;
   if (i < strlen(s))
     goto loop;
 done:
}
```

- `strlen` executed every iteration

Calling Strlen

```
/* My version of strlen */
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
       s++;
       length++;
    }
    return length;
}
```

- **Strlen performance**
  - Only way to determine length of string is to scan its entire length, looking for null character.
- **Overall performance, string of length N**
  - N calls to strlen
  - Require times N, N-1, N-2, …, 1
  - Overall O(N^2) performance

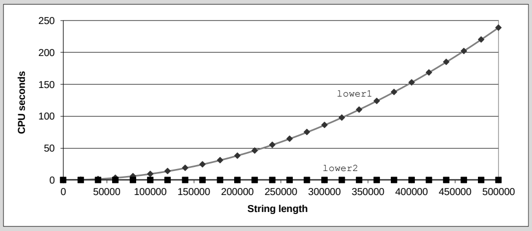
Improving Performance

```
void lower(char *s)
{
  size_t i;
  size_t len = strlen(s);
  for (i = 0; i < len; i++)
    if (s[i] >= 'A' && s[i] <= 'Z')
      s[i] -= ('A' - 'a');
}
```

- Move call to `strlen` outside of loop
- Since result does not change from one iteration to another
- Form of code motion

Lower Case Conversion Performance

- Time doubles when double string length
- Linear performance of lower2



Optimization Blocker: Procedure Calls

- ***Why couldn't compiler move `strlen` out of inner loop?***
  - Procedure may have side effects
    - Alters global state each time called
  - Function may not return same value for given arguments
    - Depends on other parts of global state
    - Procedure `lower` could interact with `strlen`
- **Warning:**
  - Compiler treats procedure call as a black box
  - Weak optimizations near them
- **Remedies:**
  - Use of inline functions
    - GCC does this with –O1
      - Within single file
      - But doesn't help here
  - Do your own code motion

```
size_t lencnt = 0;
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
       s++; length++;
    }
    lencnt += length;
    return length;
}
```

What About Larger Programs?

- **If your program has just one loop, it's obvious where to change to make it go faster**
- **In more complex programs, *what* to optimize is a key question**
- **When you first write a non-trivial program, it often has a single major algorithm performance problem**
  - Textbook's example: insertion sort
  - A program I wrote recently: missed opportunity for dynamic programming
  - Fixing this problem is way more important than any other changes

Amdahl's Law

- **If you speed up one part of a system, the total benefit is limited by how much time that part took to start with**
- **Speedup S is:**

$$S = \frac{1}{(1 - \alpha) + \alpha/k}$$

where the acceleration factor is k and the original time fraction is α.

- **Limiting case: even if k is effectively infinite, the upper limit on speedup is**

$$S_\infty = \frac{1}{(1 - \alpha)}$$

Knowing What's Slow: Profiling

- **Profiling makes a version of a program that records how long it spends on different tasks**
  - Use to find bottlenecks, at least in typical operation
- **Common Linux tools:**
  - **`gprof`**: GCC flag plus a tool to interpret output of the profiled program
    - Counts functions and randomly samples for time
    - Discussed in textbook's 5.14.1
  - Valgrind **`callgrind`**/**`cachegrind`**
    - Counts everything, precise but slow
  - OProfile
    - Uses hardware performance counters, can be whole-system

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Exercise Break: Weird Pointers

- **Can the following function ever return 12, and if so how?**

```
int f(int *p1, int *p2, int *p3) {
    *p1 = 100;
    *p2 = 10;
    *p3 = 1;
    return *p1 + *p2 + *p3;
}
```

- **Yes, for instance:**

```
int a, b;
f(&a, &b, &a);
```

https://chimein.cla.umn.edu/course/view/2021

Memory Matters

```
/* Sum rows of n X n matrix a
   and store in vector b  */
void sum_rows1(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        b[i] = 0;
        for (j = 0; j < n; j++)
            b[i] += a[i*n + j];
    }
}
```

```
# sum_rows1 inner loop
.L4:
        movsd   (%rsi,%rax,8), %xmm0       # FP load
        addsd   (%rdi), %xmm0              # FP add
        movsd   %xmm0, (%rsi,%rax,8)       # FP store
        addq    $8, %rdi
        cmpq    %rcx, %rdi
        jne     .L4
```

- Code updates `b[i]` on every iteration
- Why couldn't compiler optimize this away?

Memory Aliasing

```
/* Sum rows of n X n matrix a
   and store in vector b  */
void sum_rows1(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        b[i] = 0;
        for (j = 0; j < n; j++)
            b[i] += a[i*n + j];
    }
}
```

```
double A[9] =
  { 0,   1,   2,
    4,   8,  16},
   32,  64, 128};

double B[3] = A+3;

sum_rows1(A, B, 3);
```

Value of `B`:

```
init:  [4, 8, 16]
i = 0: [3, 8, 16]
i = 1: [3, 22, 16]
i = 2: [3, 22, 224]
```

- Code updates `b[i]` on every iteration
- Must consider possibility that these updates will affect program behavior

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Removing Aliasing

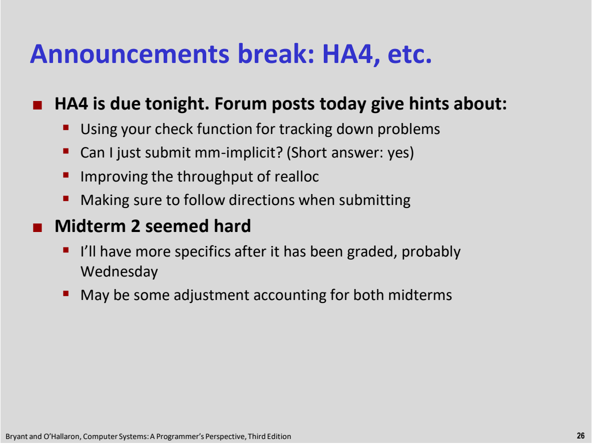
```
/* Sum rows of n X n matrix a
   and store in vector b  */
void sum_rows2(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        double val = 0;
        for (j = 0; j < n; j++)
            val += a[i*n + j];
        b[i] = val;
    }
}
```

```
# sum_rows2 inner loop
.L10:
        addsd   (%rdi), %xmm0       # FP load + add
        addq    $8, %rdi
        cmpq    %rax, %rdi
        jne     .L10
```

- No need to store intermediate results

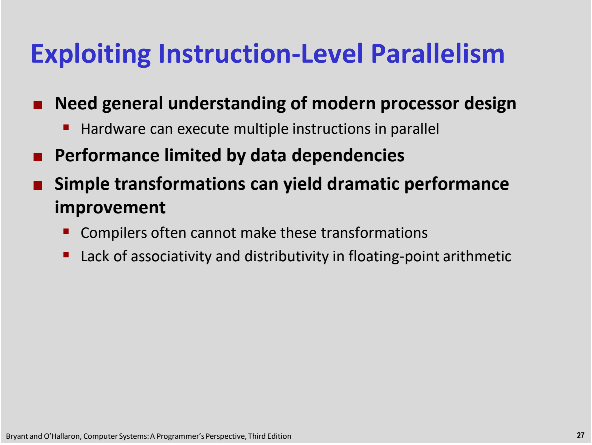
Optimization Blocker: Memory Aliasing

- **Aliasing**
  - Two different memory references specify single location
  - Easy to have happen in C
    - Since allowed to do address arithmetic
    - Direct access to storage structures
  - Get in habit of introducing local variables
    - Accumulating within loops
    - Your way of telling compiler aliasing is impossible



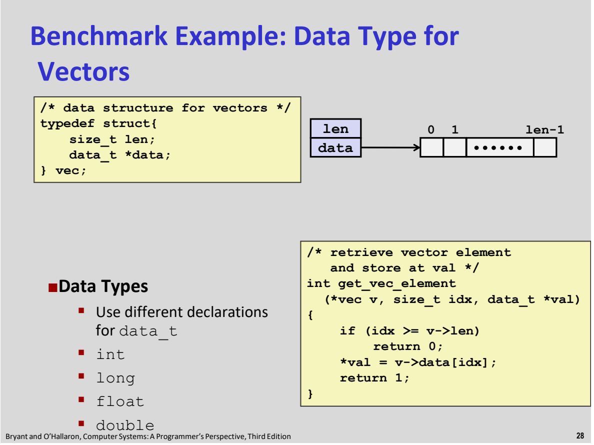
Announcements break: HA4, etc.

- **HA4 is due tonight. Forum posts today give hints about:**
  - Using your check function for tracking down problems
  - Can I just submit mm-implicit? (Short answer: yes)
  - Improving the throughput of realloc
  - Making sure to follow directions when submitting
- **Midterm 2 seemed hard**
  - I'll have more specifics after it has been graded, probably Wednesday
  - May be some adjustment accounting for both midterms



Exploiting Instruction-Level Parallelism

- **Need general understanding of modern processor design**
  - Hardware can execute multiple instructions in parallel
- **Performance limited by data dependencies**
- **Simple transformations can yield dramatic performance improvement**
  - Compilers often cannot make these transformations
  - Lack of associativity and distributivity in floating-point arithmetic

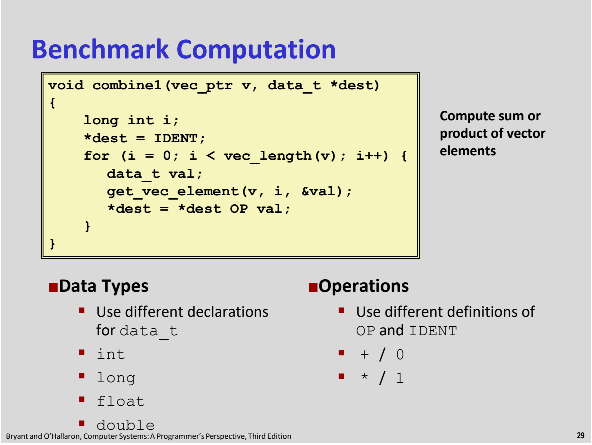


Benchmark Example: Data Type for Vectors

```
/* data structure for vectors */
typedef struct{
    size_t len;
    data_t *data;
} vec;
```

```
/* retrieve vector element
   and store at val */
int get_vec_element
  (*vec v, size_t idx, data_t *val)
{
    if (idx >= v->len)
        return 0;
    *val = v->data[idx];
    return 1;
}
```

- **Data Types**
  - Use different declarations for `data_t`
  - `int`
  - `long`
  - `float`
  - `double`

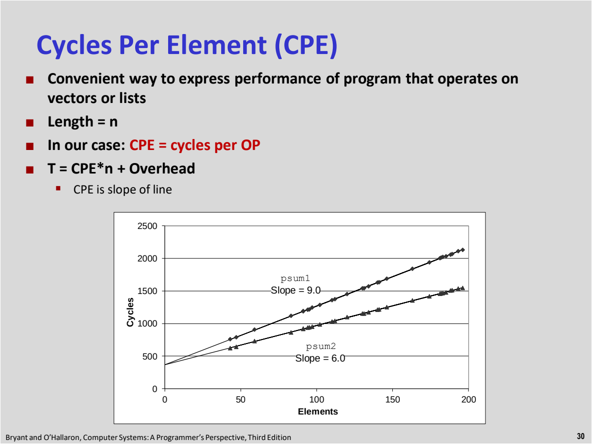


Benchmark Computation

```
void combine1(vec_ptr v, data_t *dest)
{
    long int i;
    *dest = IDENT;
    for (i = 0; i < vec_length(v); i++) {
       data_t val;
       get_vec_element(v, i, &val);
       *dest = *dest OP val;
    }
}
```

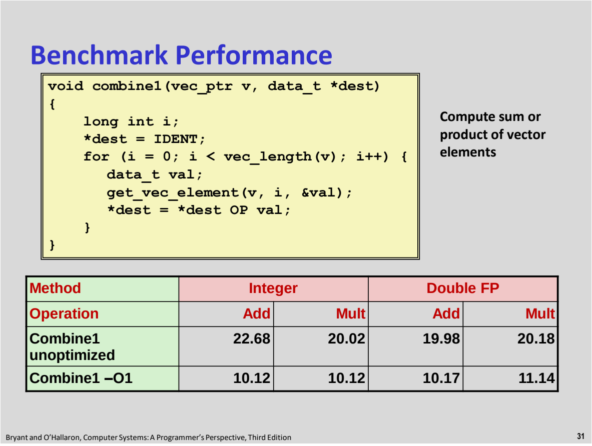
Compute sum or product of vector elements

- **Data Types**
  - Use different declarations for `data_t`
  - `int`
  - `long`
  - `float`
  - `double`
- **Operations**
  - Use different definitions of `OP` and `IDENT`
  - `+ / 0`
  - `* / 1`



Cycles Per Element (CPE)

- **Convenient way to express performance of program that operates on vectors or lists**
- **Length = n**
- **In our case: CPE = cycles per OP**
- **T = CPE*n + Overhead**
  - CPE is slope of line



Benchmark Performance

```
void combine1(vec_ptr v, data_t *dest)
{
    long int i;
    *dest = IDENT;
    for (i = 0; i < vec_length(v); i++) {
       data_t val;
       get_vec_element(v, i, &val);
       *dest = *dest OP val;
    }
}
```

Compute sum or product of vector elements

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine1 unoptimized	22.68	20.02	19.98	20.18
Combine1 –O1	10.12	10.12	10.17	11.14

Basic Optimizations

```
void combine4(vec_ptr v, data_t *dest)
{
  long i;
  long length = vec_length(v);
  data_t *d = get_vec_start(v);
  data_t t = IDENT;
  for (i = 0; i < length; i++)
    t = t OP d[i];
  *dest = t;
}
```

- Move vec_length out of loop
- Avoid bounds check on each cycle
- Accumulate in temporary

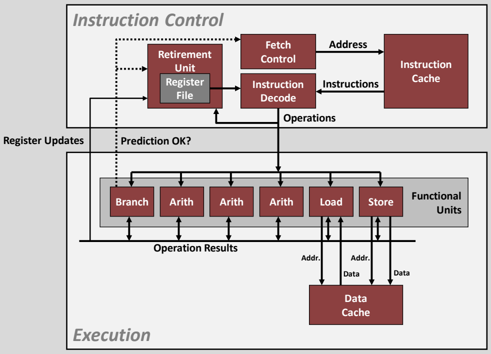
Effect of Basic Optimizations

```
void combine4(vec_ptr v, data_t *dest)
{
  long i;
  long length = vec_length(v);
  data_t *d = get_vec_start(v);
  data_t t = IDENT;
  for (i = 0; i < length; i++)
    t = t OP d[i];
  *dest = t;
}
```

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine1 –O1	10.12	10.12	10.17	11.14
Combine4	1.27	3.01	3.01	5.01

- Eliminates sources of overhead in loop

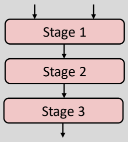
Modern CPU Design



Superscalar Processor

- **Definition:** A superscalar processor can issue and execute *multiple instructions in one cycle*. The instructions are retrieved from a sequential instruction stream and are usually scheduled dynamically.
- Benefit: without programming effort, superscalar processor can take advantage of the *instruction level parallelism* that most programs have
- Most modern CPUs are superscalar.
- Intel: since Pentium (1993)

Pipelined Functional Units



```
long mult_eg(long a, long b, long c) {
    long p1 = a*b;
    long p2 = a*c;
    long p3 = p1 * p2;
    return p3;
}
```

	Time						
	1	2	3	4	5	6	7
Stage 1	`a*b`	`a*c`			`p1*p2`		
Stage 2		`a*b`	`a*c`			`p1*p2`	
Stage 3			`a*b`	`a*c`			`p1*p2`

- Divide computation into stages
- Pass partial computations from stage to stage
- Stage i can start on new computation once values passed to i+1
- E.g., complete 3 multiplications in 7 cycles, even though each requires 3 cycles

---

Haswell CPU

  - 8 Total Functional Units
- Multiple instructions can execute in parallel

2 load, with address computation
1 store, with address computation
4 integer
2 FP multiply
1 FP add
1 FP divide

- Some instructions take > 1 cycle, but can be pipelined

Instruction	*Latency*	*Cycles/Issue*
Load / Store	4	1
Integer Multiply	3	1
Integer/Long Divide	**3-30**	**3-30**
Single/Double FP Multiply	5	1
Single/Double FP Add	3	1
Single/Double FP Divide	**3-15**	**3-15**

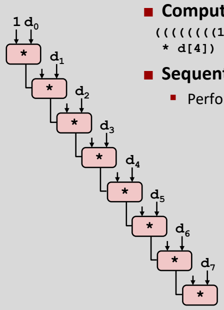
x86-64 Compilation of Combine4

- **Inner Loop (Case: Integer Multiply)**

```
.L519:                           # Loop:
  imull  (%rax,%rdx,4), %ecx     # t = t * d[i]
  addq   $1, %rdx                # i++
  cmpq   %rdx, %rbp              # Compare length:i
  jg     .L519                   # If >, goto Loop
```

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine4	1.27	3.01	3.01	5.01
Latency Bound	1.00	3.00	3.00	5.00

Combine4 = Serial Computation (OP = *)



- **Computation (length=8)**

```
((((((((1 * d[0]) * d[1]) * d[2]) * d[3])
 * d[4]) * d[5]) * d[6]) * d[7])
```

- **Sequential dependence**
  - Performance: determined by latency of OP

Loop Unrolling (2x1)

```
void unroll2a_combine(vec_ptr v, data_t *dest)
{
    long length = vec_length(v);
    long limit = length-1;
    data_t *d = get_vec_start(v);
    data_t x = IDENT;
    long i;
    /* Combine 2 elements at a time */
    for (i = 0; i < limit; i+=2) {
        x = (x OP d[i]) OP d[i+1];
    }
    /* Finish any remaining elements */
    for (; i < length; i++) {
        x = x OP d[i];
    }
    *dest = x;
}
```

- **Perform 2x more useful work per iteration**

Effect of Loop Unrolling

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine4	1.27	3.01	3.01	5.01
Unroll 2x1	1.01	3.01	3.01	5.01
Latency Bound	1.00	3.00	3.00	5.00

- **Helps integer add**
  - Achieves latency bound
- **Others don't improve. *Why?***
  - Still sequential dependency

`x = (x OP d[i]) OP d[i+1];`

Announcements break: midterm stats

```
4 | 24
4 | 5678999
5 | 01233444
5 | 5566778899
6 | 0011111222223333344
6 | 555667788999
7 | 0001123334
7 | 55567778899999
8 | 0011234
8 | 556789
9 | 134
9 | 6
```

Midterm 2 (50-100 shown)

```
5 | 5899
6 | 0133
6 | 7888999
7 | 011122334444
7 | 55567777888999
8 | 0000001122234444
8 | 5566667777777888889
9 | 00112222233444
9 | 555668
10| 00
```

Adjusted combined midterms (50-100 shown)

Adjustment is +6 to M2 or +3 to average

More announcements

- **Midterm 2 solutions are now on the web site**
- **Exercise Set 4 on caches is posted**
  - Due in class Wednesday 11/28 a week from today

Loop Unrolling with Reassociation (2x1a)

```
void unroll2aa_combine(vec_ptr v, data_t *dest)
{
    long length = vec_length(v);
    long limit = length-1;
    data_t *d = get_vec_start(v);
    data_t x = IDENT;
    long i;
    /* Combine 2 elements at a time */
    for (i = 0; i < limit; i+=2) {
       x = x OP (d[i] OP d[i+1]);
    }
    /* Finish any remaining elements */
    for (; i < length; i++) {
       x = x OP d[i];
    }
    *dest = x;
}
```

Compare to before

`x = (x OP d[i]) OP d[i+1];`

- **Can this change the result of the computation?**
- **Yes, for FP. *Why?***

Effect of Reassociation

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine4	1.27	3.01	3.01	5.01
Unroll 2x1	1.01	3.01	3.01	5.01
Unroll 2x1a	1.01	1.51	1.51	2.51
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	0.50	1.00	1.00	0.50

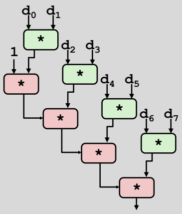
2 func. units for FP *
2 func. units for load

4 func. units for int +
2 func. units for load

- **Nearly 2x speedup for Int *, FP +, FP ***
  - Reason: Breaks sequential dependency
    `x = x OP (d[i] OP d[i+1]);`
  - Why is that? (next slide)

Reassociated Computation

`x = x OP (d[i] OP d[i+1]);`



- **What changed:**
  - Ops in the next iteration can be started early (no dependency)
- **Overall Performance**
  - N elements, D cycles latency/op
  - (N/2+1)*D cycles:
    CPE = D/2

Loop Unrolling with Separate Accumulators (2x2)

```
void unroll2a_combine(vec_ptr v, data_t *dest)
{
    long length = vec_length(v);
    long limit = length-1;
    data_t *d = get_vec_start(v);
    data_t x0 = IDENT;
    data_t x1 = IDENT;
    long i;
    /* Combine 2 elements at a time */
    for (i = 0; i < limit; i+=2) {
       x0 = x0 OP d[i];
       x1 = x1 OP d[i+1];
    }
    /* Finish any remaining elements */
    for (; i < length; i++) {
       x0 = x0 OP d[i];
    }
    *dest = x0 OP x1;
}
```

- **Different form of reassociation**

Effect of Separate Accumulators

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine4	1.27	3.01	3.01	5.01
Unroll 2x1	1.01	3.01	3.01	5.01
Unroll 2x1a	1.01	1.51	1.51	2.51
Unroll 2x2	0.81	1.51	1.51	2.51
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	0.50	1.00	1.00	0.50

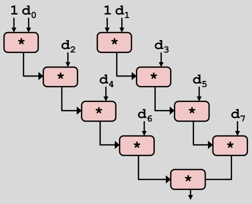
- **Int + makes use of two load units**

```
x0 = x0 OP d[i];
x1 = x1 OP d[i+1];
```

- **2x speedup (over unroll2) for Int *, FP +, FP ***

Separate Accumulators

```
x0 = x0 OP d[i];
x1 = x1 OP d[i+1];
```



- **What changed:**
  - Two independent “streams” of operations
- **Overall Performance**
  - N elements, D cycles latency/op
  - Should be (N/2+1)*D cycles:
    CPE = D/2
  - CPE matches prediction!

What Now?

Unrolling & Accumulating

- **Idea**
  - Can unroll to any degree L
  - Can accumulate K results in parallel
  - L must be multiple of K
- **Limitations**
  - Diminishing returns
    - Cannot go beyond throughput limitations of execution units
  - Large overhead for short lengths
    - Finish off iterations sequentially

Unrolling & Accumulating: Double *

- **Case**
  - Intel Haswell
  - Double FP Multiplication
  - Latency bound: 5.00. Throughput bound: 0.50

Accumulators

FP *	Unrolling Factor L							
K	1	2	3	4	6	8	10	12
1	5.01	5.01	5.01	5.01	5.01	5.01	5.01	
2		2.51		2.51		2.51		
3			1.67					
4				1.25		1.26		
6					0.84			0.88
8						0.63		
10							0.51	
12								0.52

Unrolling & Accumulating: Int +

- **Case**
  - Intel Haswell
  - Integer addition
  - Latency bound: 1.00. Throughput bound: 1.00

Accumulators

FP *	Unrolling Factor L							
K	1	2	3	4	6	8	10	12
1	1.27	1.01	1.01	1.01	1.01	1.01	1.01	
2		0.81		0.69		0.54		
3			0.74					
4				0.69		1.24		
6					0.56			0.56
8						0.54		
10							0.54	
12								0.56

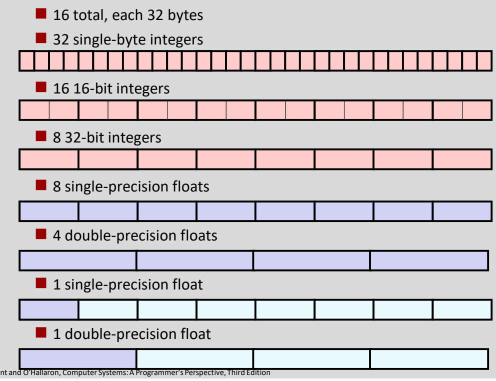
Achievable Performance

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Best	0.54	1.01	1.01	0.52
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	0.50	1.00	1.00	0.50

- **Limited only by throughput of functional units**
- **Up to 42X improvement over original, unoptimized code**

Programming with AVX2

YMM Registers

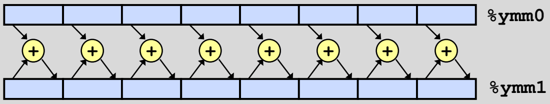


- 16 total, each 32 bytes
- 32 single-byte integers
- 16 16-bit integers
- 8 32-bit integers
- 8 single-precision floats
- 4 double-precision floats
- 1 single-precision float
- 1 double-precision float

SIMD Operations

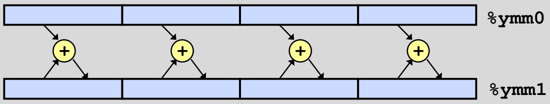
- SIMD Operations: Single Precision

```
vaddsd %ymm0, %ymm1, %ymm1
```



- SIMD Operations: Double Precision

```
vaddpd %ymm0, %ymm1, %ymm1
```



Using Vector Instructions

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Scalar Best	0.54	1.01	1.01	0.52
Vector Best	0.06	0.24	0.25	0.16
Latency Bound	0.50	3.00	3.00	5.00
Throughput Bound	0.50	1.00	1.00	0.50
Vec Throughput Bound	0.06	0.12	0.25	0.12

- **Make use of AVX Instructions**
  - Parallel operations on multiple data elements
  - See Web Aside OPT:SIMD on CS:APP web page

What About Branches?

- **Challenge**
  - Instruction Control Unit must work well ahead of Execution Unit to generate enough operations to keep EU busy

```
404663:  mov    $0x0,%eax
404668:  cmp    (%rdi),%rsi
40466b:  jge    404685
40466d:  mov    0x8(%rdi),%rax

  . . .

404685:  repz retq
```

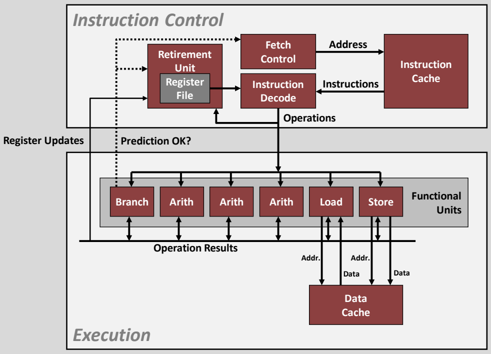
Executing

How to continue?

- When encounters conditional branch, cannot reliably determine where to continue fetching

---

Modern CPU Design



Branch Outcomes

- **When encounter conditional branch, cannot determine where to continue fetching**
  - Branch Taken: Transfer control to branch target
  - Branch Not-Taken: Continue with next instruction in sequence
- **Cannot resolve until outcome determined by branch/integer unit**

```
404663:  mov    $0x0,%eax
404668:  cmp    (%rdi),%rsi
40466b:  jge    404685
40466d:  mov    0x8(%rdi),%rax

  . . .

404685:  repz retq
```

Branch Not-Taken

Branch Taken

Branch Prediction

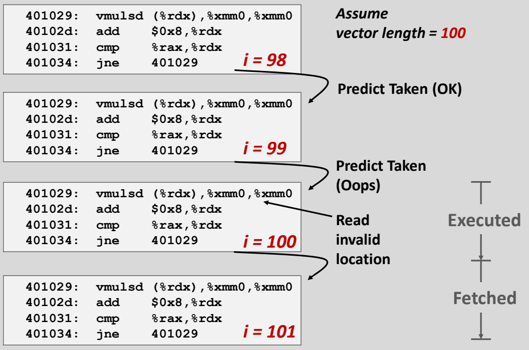
- **Idea**
  - Guess which way branch will go
  - Begin executing instructions at predicted position
    - But don't actually modify register or memory data

```
404663:  mov    $0x0,%eax
404668:  cmp    (%rdi),%rsi
40466b:  jge    404685
40466d:  mov    0x8(%rdi),%rax

  . . .

404685:  repz retq
```

Predict Taken

Begin Execution

Branch Prediction Through Loop



```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

i = 98

```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

i = 99

```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

i = 100

```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

i = 101

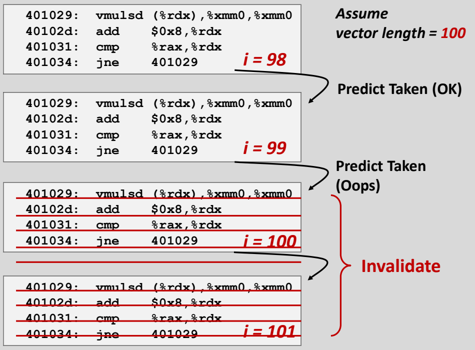
Assume vector length = 100

Predict Taken (OK)

Predict Taken (Oops)

Read invalid location

Branch Misprediction Invalidation



Assume
vector length = 100

```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

i = 98

Predict Taken (OK)

```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

i = 99

Predict Taken
(Oops)

```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

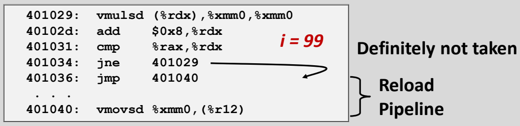
~~*i = 100*~~

```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
```

~~*i = 101*~~

Invalidate

Branch Misprediction Recovery



```
401029:  vmulsd (%rdx),%xmm0,%xmm0
40102d:  add    $0x8,%rdx
401031:  cmp    %rax,%rdx
401034:  jne    401029
401036:  jmp    401040
  . . .
401040:  vmovsd %xmm0,(%r12)
```

i = 99

Definitely not taken

Reload
Pipeline

- **Performance Cost**
  - Multiple clock cycles on modern processor
  - Can be a major performance limiter

Effect of Branch Prediction: Good News

- **Loops**
  - Typically, only miss when hit loop end
- **Checking code**
  - Reliably predicts that error won't occur

```
void combine4b(vec_ptr v,
               data_t *dest)
{
    long int i;
    long int length = vec_length(v);
    data_t acc = IDENT;
    for (i = 0; i < length; i++) {
      if (i >= 0 && i < v->len) {
          acc = acc OP v->data[i];
      }
    }
    *dest = acc;
}
```

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Combine4b	4.0	4.0	4.0	5.0

Branch Prediction: Bad News

- **Some program branches are inherently unpredictable**
  - E.g., if based on input data, binary search tree, etc.
  - Indirect jumps are also often hard to predict
- **These can be a major performance bottleneck**
  - Misprediction penalty is typically 10-20 cycles
- **Partial solution: write code to be compiled to conditional moves**
  - For GCC: use math and `? :` instead of `if`
  - Textbook gives min/max and mergesort examples

Getting High Performance

- **Good compiler and flags**
- **Don't do anything stupid**
  - Watch out for hidden algorithmic inefficiencies
  - Write compiler-friendly code
    - Watch out for optimization blockers: procedure calls & memory references
  - Look carefully at innermost loops (where most work is done)

- **Tune code for machine**
  - Exploit instruction-level parallelism
  - Avoid unpredictable branches
  - Make code cache friendly (Covered later in course)