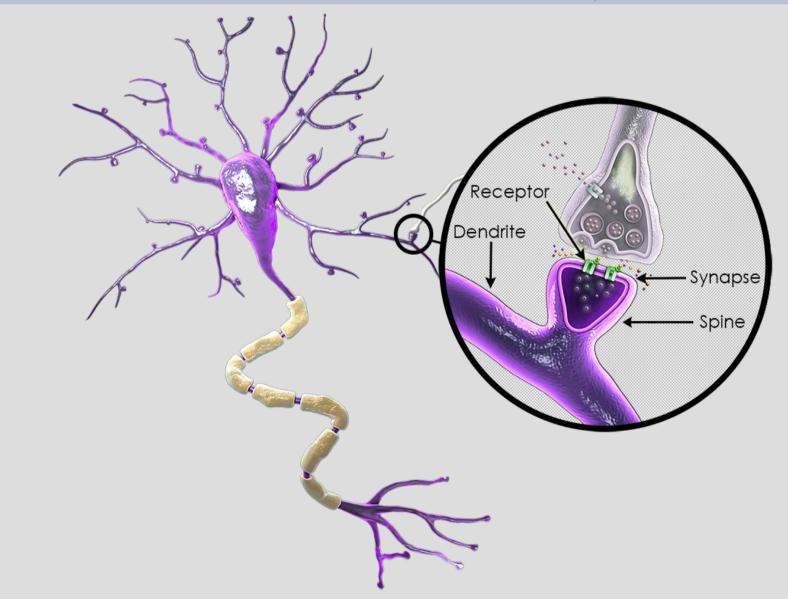
#### Neural networks (Ch. 12)

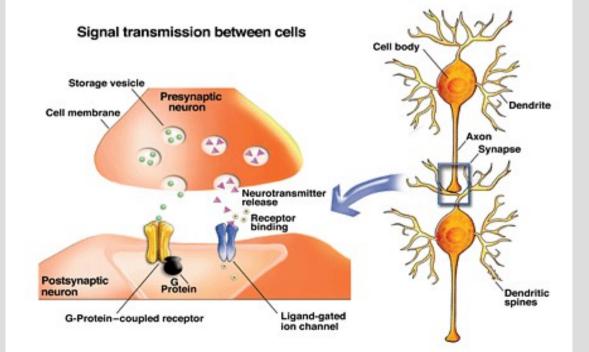


Computer science is fundamentally a creative process: building new & interesting algorithms

As with other creative processes, this involves mixing ideas together from various places

Neural networks get their inspiration from how brains work at a fundamental level (simplification... of course)

(Disclaimer: I am **not** a neuroscience-person) Brains receive small chemical signals at the "input" side, if there are enough inputs to "activate" it signals an "output"



An analogy is sleeping: when you are asleep, minor sounds will not wake you up

# However, specific sounds in combination with their volume will wake you up



Other sounds might help you go to sleep (my majestic voice?)

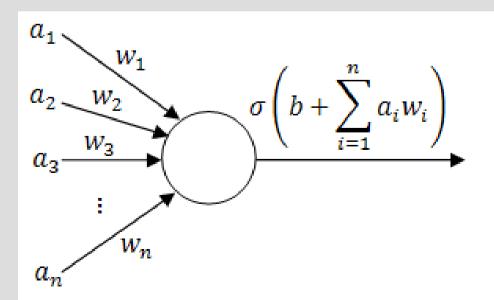
Many babies tend to sleep better with "white noise" and some people like the TV/radio on



#### Neural network: basics

Neural networks are connected nodes, which can be arranged into layers (more on this later)

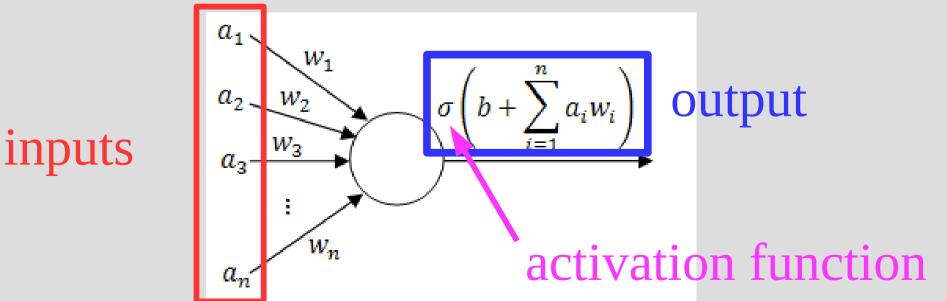
First is an example of a perceptron, the most simple NN; a single node on a single layer



#### Neural network: basics

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#### Mammals

Let's do an example with mammals...

First the definition of a mammal (wikipedia):

Mammals [posses]:

- (1) a neocortex (a region of the brain),(2) hair,
- (3) three middle ear bones,
- (4) and mammary glands

#### Mammals

Common mammal misconceptions: (1) Warm-blooded (2) Does not lay eggs

#### Let's talk dolphins for one second.

http://mentalfloss.com/article/19116/if-dolphins-are-mammals-and-all-mammals-have-hair-why-arent-dolphins-hairy

Dolphins have hair (technically) for the first week after birth, then lose it for the rest of life ... I will count this as "not covered in hair"

Consider this example: we want to classify whether or not an animal is mammal via a perceptron (weighted evaluation)

We will evaluate on: 1. Warm blooded? (WB) Weight = 2 2. Lays eggs? (LE) Weight = -2 3. Covered hair? (CH) Weight = 3

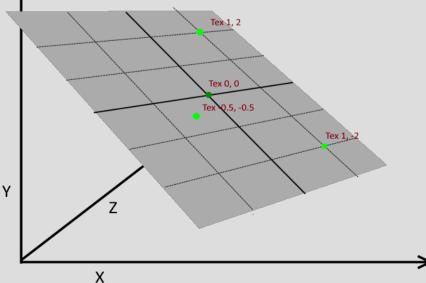
 $If(2 \cdot WB + -2 \cdot LE + 3 \cdot CH > 1) \Rightarrow Mammal$ 

Consider the following animals: Humans {WB=y, LE=n, CH=y}, mam=y  $2(1) + -2(-1) + 3(1) = 7 > 1 \dots$  Correct! Bat {WB=sorta, LE=n, CH=y}, mam=y  $2(0.5) + -2(-1) + 3(1) = 6 > 1 \dots$  Correct! What about these? Platypus {WB=y, LE=y, CH=y}, mam=y Dolphin {WB=y, LE=n, CH=n}, mam=y Fish {WB=n, LE=y, CH=n}, mam=n Birds {WB=y, LE=y, CH=n}, mam=n

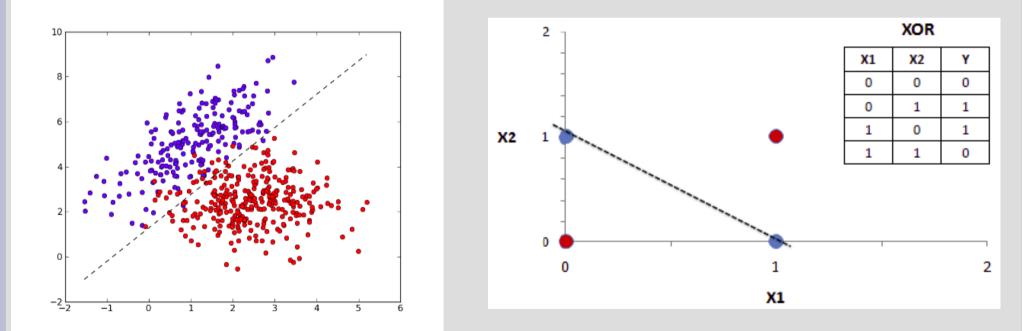
#### But wait... what is the general form of: $w_1x + w_2 \cdot y + w_3 \cdot z > c$

But wait... what is the general form of:  $w_1x + w_2 \cdot y + w_3 \cdot z > c$ 

This is simply one side of a plane in 3D, so this is trying to classify all possible points using a single plane...



If we had only 2 inputs, it would be everything above a line in 2D, but consider XOR on right



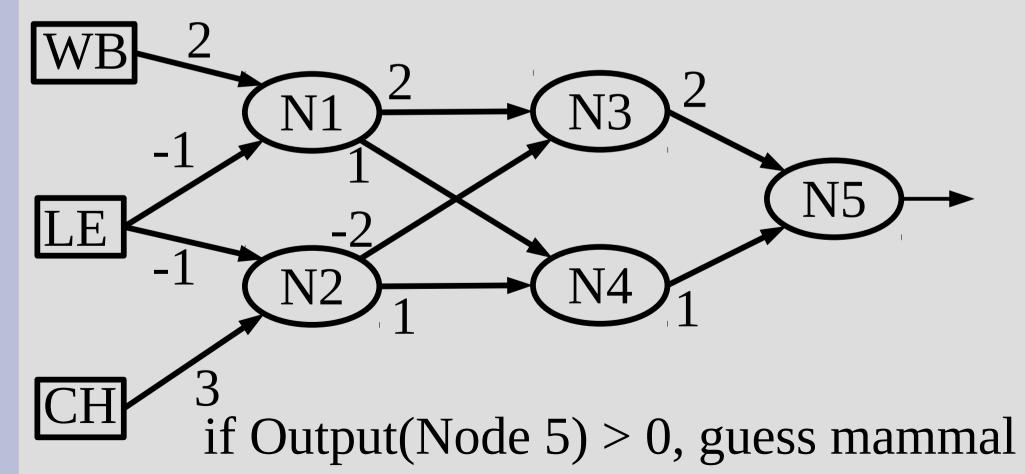
There is no way a line can possibly classify this (limitation of perceptron)

Today we will look at <u>feed-forward</u> NN, where information flows in a single direction

<u>Recurrent</u> networks can have outputs of one node loop back to inputs as previous

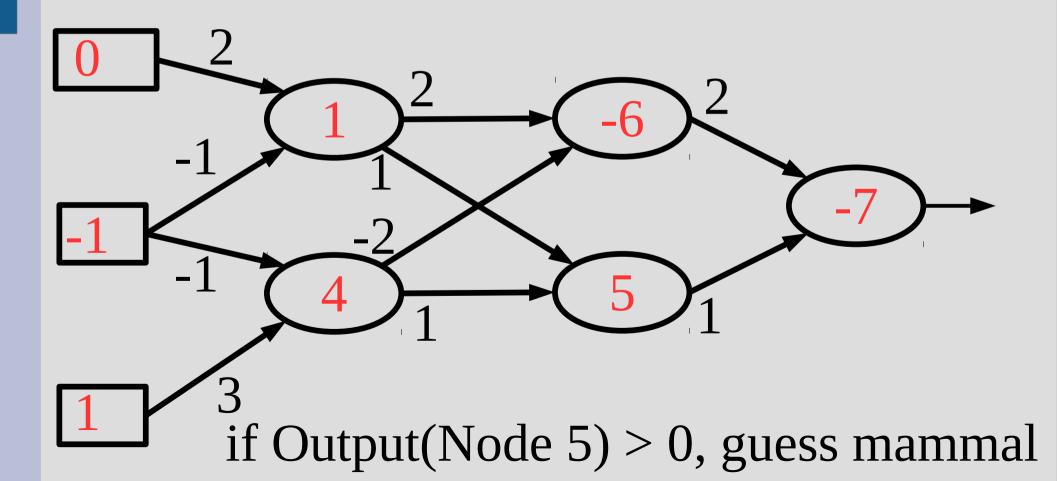
This can cause the NN to not converge on an answer (ask it the same question and it will respond differently) and also has to maintain some "initial state" (all around messy)

Let's expand our mammal classification to 5 nodes in 3 layers (weights on edges):



You try Bat on this:{WB=0, LE=-1, CH=1} Assume (for now) output = sum input if Output(Node 5) > 0, guess mammal

Output is -7, so bats are not mammal... Oops...

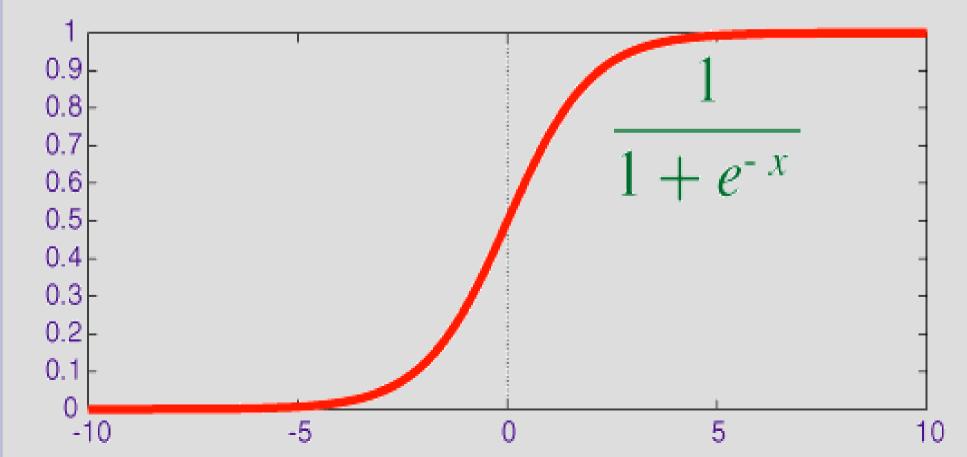


In fact, this is no better than our 1 node NN

This is because we simply output a linear combination of weights into a linear function (i.e. if f(x) and g(x) are linear... then g(x)+f(x) is also linear)

Ideally, we want a activation function that has a limited range so large signals do not always dominate

One commonly used function is the sigmoid:  $S(x) = \frac{1}{1+e^{-x}}$ 



The neural network is as good as it's structure and weights on edges

Structure we will ignore (more complex), but there is an automated way to learn weights

Whenever a NN incorrectly answer a problem, the weights play a "blame game"...

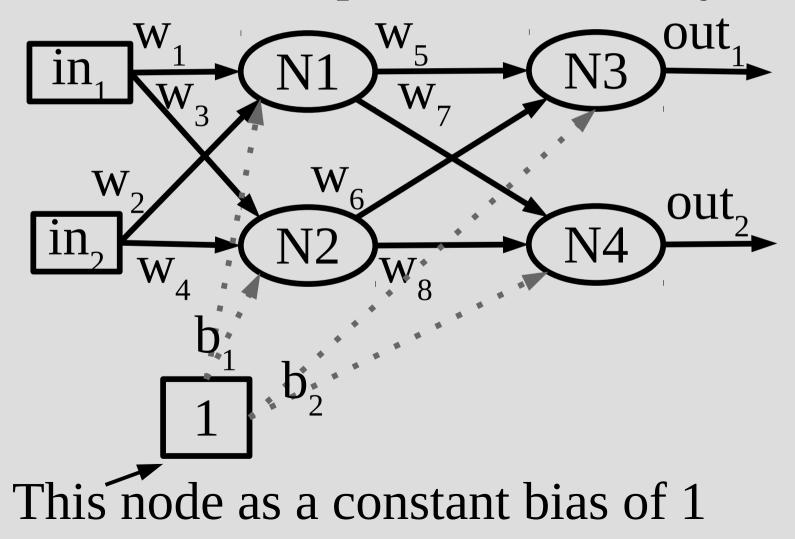
- Weights that have a big impact to the wrong answer are reduced

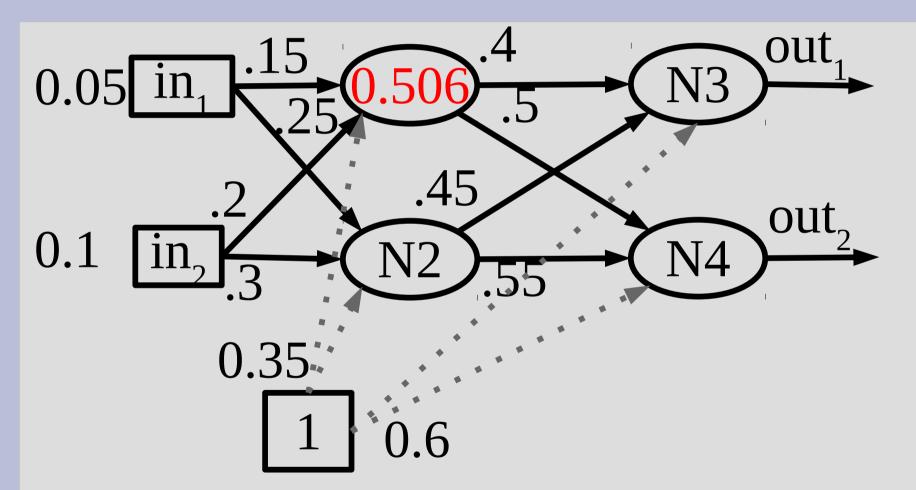
To do this blaming, we have to find how much each weight influenced the final answer

Steps:

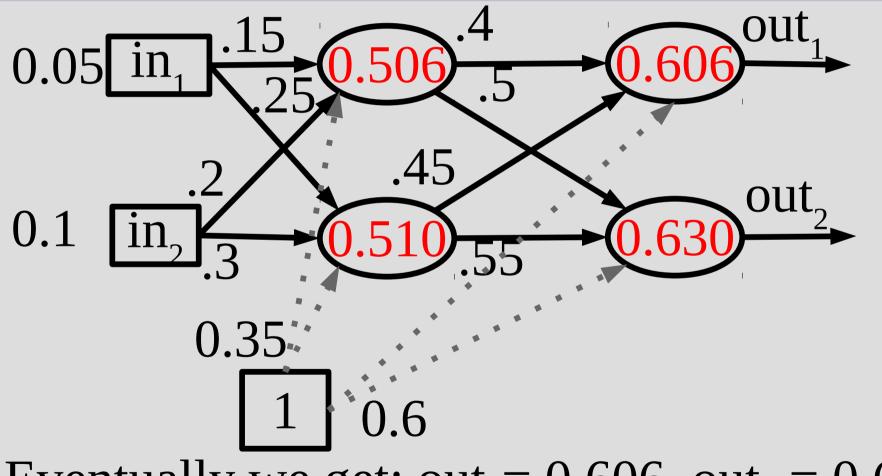
- 1. Find total error
- 2. Find derivative of error w.r.t. weights
- 3. Penalize each weight by an amount proportional to this derivative

#### Consider this example: 4 nodes, 2 layers





Node 1: 0.15\*0.05 + 0.2\*0.1 = 0.35 as input thus it outputs (all edges) S(0.35)=0.59327



Eventually we get:  $out_1 = 0.606$ ,  $out_2 = 0.630$ Suppose wanted:  $out_1 = 0.01$ ,  $out_2 = 0.99$ 

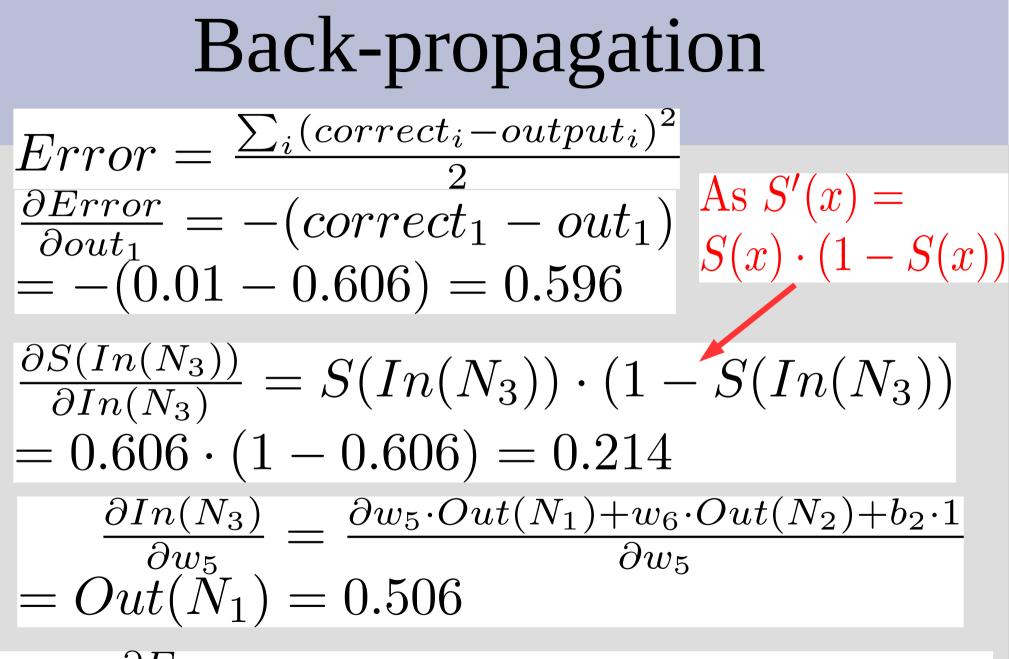
We will define the error as:  $\frac{\sum_{i} (correct_{i} - output_{i})^{2}}{2}$ 

Suppose we want to find how much  $W_5$  is to blame for our incorrectness

We then need to find: Apply the chain rule:

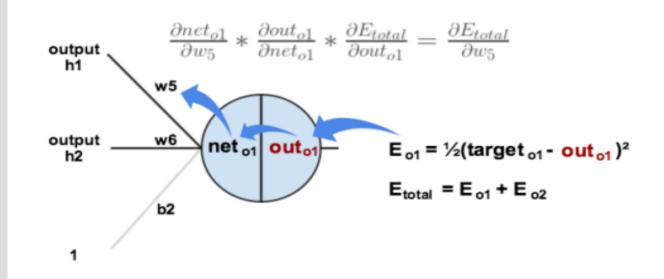
$$rac{\partial Error}{\partial w_5}$$

$$\frac{\partial Error}{\partial out_1} \cdot \frac{\partial S(In(N_3))}{\partial In(N_3)} \cdot \frac{\partial In(N_3)}{\partial w_5}$$



Thus,  $\frac{\partial Error}{\partial w_5} = 0.596 \cdot 0.214 \cdot 0.506 = 0.0645$ 

#### In a picture we did this:



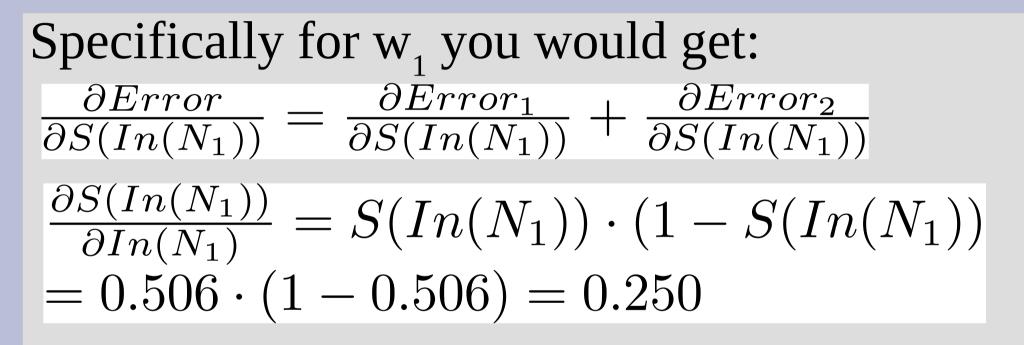
Now that we know w5 is 0.08217 part responsible, we update the weight by:  $w_5 \leftarrow w_5 - \alpha * 0.0645 = 0.374$  (from 0.4)  $\alpha$  is learning rate, set to 0.5

Updating this  $w_5$  to  $w_8$  gives:  $w_5 = 0.3589$   $w_6 = 0.4067$   $w_7 = 0.5113$  $w_8 = 0.5614$ 

For other weights, you need to consider all possible ways in which they contribute

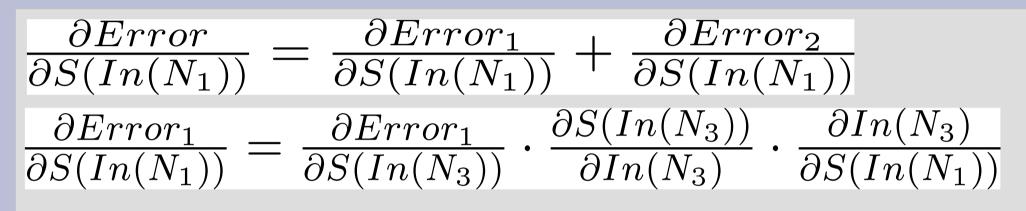
#### For w<sub>1</sub> it would look like: $\frac{\partial E_{total}}{\partial w_1} = \frac{\partial E_{total}}{\partial out_{h_1}} * \frac{\partial out_{h_1}}{\partial net_{h_1}} * \frac{\partial net_{h_1}}{\partial w_1}$ $\frac{\partial E_{total}}{\partial out_{b1}} = \frac{\partial E_{o1}}{\partial out_{b1}} + \frac{\partial E_{o2}}{\partial out_{b1}}$ h1 E .2 i2 h2 $E_{total} = E_{01} + E_{02}$ b2 1

#### (book describes how to dynamic program this)



$$\frac{\partial In(N_3)}{\partial w_5} = \frac{\partial w_1 \cdot In_1 + w_2 \cdot In_2 + b_1 \cdot 1}{\partial w_5}$$
$$= In_1 = 0.05$$

Next we have to break down the top equation...



From before...  $\frac{\partial Error_1}{\partial S(In(N_3))} \cdot \frac{\partial S(In(N_3))}{\partial In(N_3)}$ = 0.596 \cdot 0.214 = 0.128

 $\frac{\partial In(N_3)}{\partial S(In(N_1))} = \frac{\partial w_5 \cdot S(In(N_1)) + w_6 \cdot S(In(N_2)) + b_1 \cdot 1)}{\partial S(In(N_1))}$  $= w_5 = 0.4$ 

Thus,  $\frac{\partial Error_1}{\partial S(In(N_1))} = 0.128 \cdot 0.4 = 0.0510$ 

#### Similarly for Error<sub>2</sub> we get:

 $\frac{\partial Error}{\partial S(In(N_1))} = \frac{\partial Error_1}{\partial S(In(N_1))} + \frac{\partial Error_2}{\partial S(In(N_1))} \\ = 0.0510 + -0.0190 = 0.0320$ 

Thus,  $\frac{\partial Error}{\partial w_1} = 0.0320 \cdot 0.250 \cdot 0.05 = 0.000400$ 

Update  $w_1 \leftarrow w_1 - \alpha \frac{\partial Error}{\partial w_1} = 0.15 - 0.5 \cdot 0.0004 = 0.1498$ 

You might notice this is small... This is an issue with neural networks, deeper the network the less earlier nodes update