# **Cache Memories**

CSci 2021: Machine Architecture and Organization April 1st-3rd, 2020

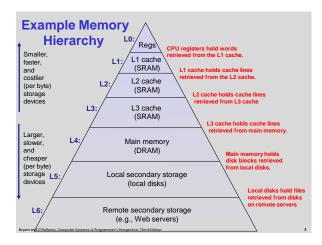
Your instructor: Stephen McCamant

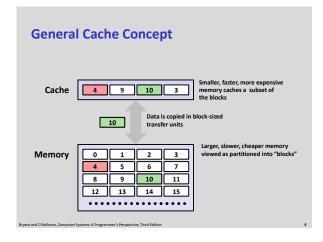
**Based on slides originally by:** Randy Bryant, Dave O'Hallaron

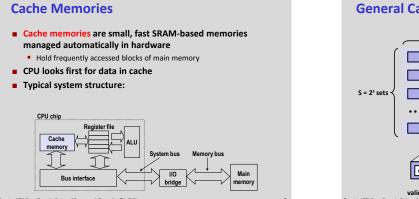
### **Today**

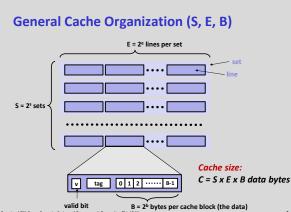
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- Cache memory organization and operation
  - Performance impact of caches
  - The memory mountain
  - Rearranging loops to improve spatial locality
  - Using blocking to improve temporal locality

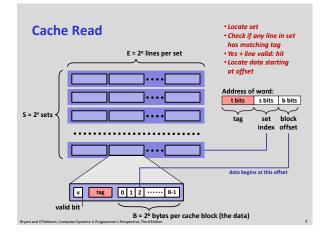


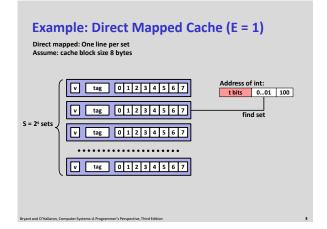






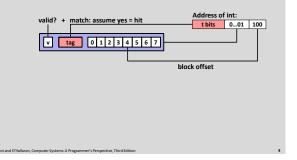
# 1

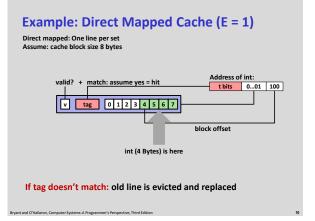


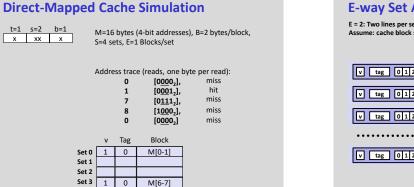


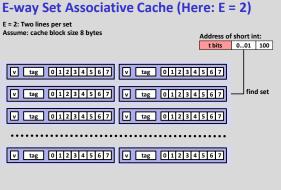
Example: Direct Mapped Cache (E = 1)

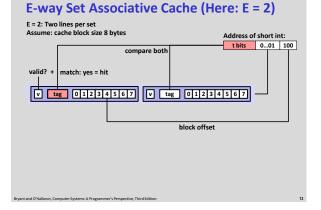
Direct mapped: One line per set Assume: cache block size 8 bytes



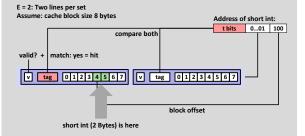






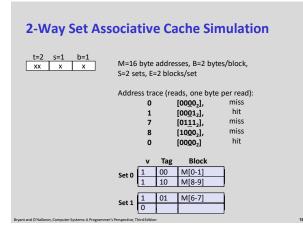


# E-way Set Associative Cache (Here: E = 2)



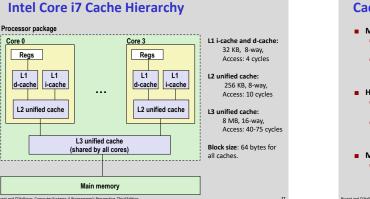
### No match:

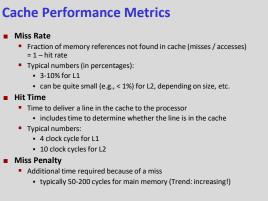
- · One line in set is selected for eviction and replacement
- · Replacement policies: random, least recently used (LRU), ...



Core 0

## What about writes? Multiple copies of data exist: L1, L2, L3, Main Memory, Disk What to do on a write-hit? Write-through (write immediately to memory) Write-back (defer write to memory until replacement of line) Need a dirty bit (line different from memory or not) What to do on a write-miss? Write-allocate (load into cache, update line in cache) Good if more writes to the location follow No-write-allocate (writes straight to memory, does not load into cache) Typical Write-through + No-write-allocate Write-back + Write-allocate



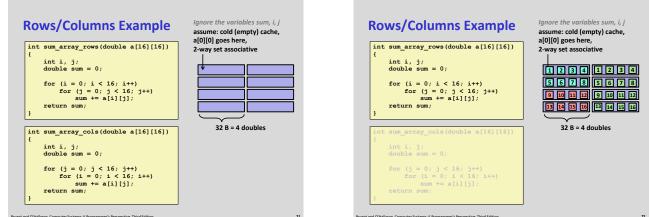


# Let's think about those numbers Huge difference between a hit and a miss Could be 100x, if just L1 and main memory Would you believe 99% hits is twice as good as 97%? Consider: cache hit time of 1 cycle miss penalty of 100 cycles Average access time: 97% hits: 1 cycle + 0.03 \* 100 cycles = 4 cycles 99% hits: 1 cycle + 0.01 \* 100 cycles = 2 cycles This is why "miss rate" is used instead of "hit rate"

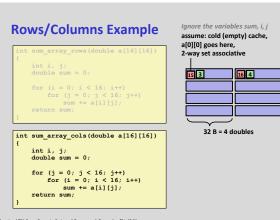
# Writing Cache Friendly Code

- Make the common case go fast
- Focus on the inner loops of the core functions
- Minimize the misses in the inner loops
  - Repeated references to variables are good (temporal locality)
  - Stride-1 reference patterns are good (spatial locality)

Key idea: Our qualitative notion of locality is quantified through our understanding of cache memories



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15 3	16 4

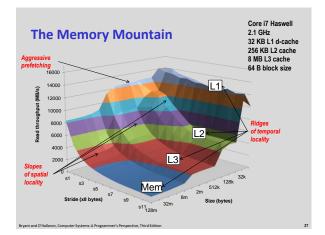
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- Performance impact of caches
  - The memory mountain
  - Rearranging loops to improve spatial locality
  - Using blocking to improve temporal locality

### **The Memory Mountain**

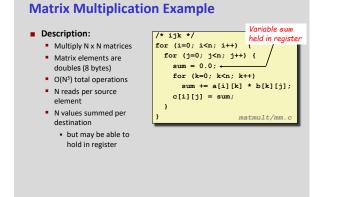
- Read throughput (read bandwidth)
   Number of bytes read from memory per second (MB/s)
- Memory mountain: Measured read throughput as a function of spatial and temporal locality.
  - Compact way to characterize memory system performance.

### **Memory Mountain Test Function** long data[MAXELEMS]; /\* Global array to traverse \*/ /\* test - Iterate over first "elems" elements of \* array "data" with stride of "stride", using \* using 4x4 loop unrolling. Call test() with many combinations of elems and stride. int test(int elems, int stride) { long i, sx2=stride\*2, sx3=stride\*3, sx4=stride\*4; long acc0 = 0, acc2 = 0, acc2 = 0; long length = elems, limit = length - sx4; For each elems and stride: 1. Call test() Combine 4 elements at a time \*/ once to warm up for (i = 0; i < limit; i += sx4) { the caches. or (i = 0; i < limit; i += sx4) { acc0 = acc0 + data[i]; acc1 = acc1 + data[i+stride]; acc2 = acc2 + data[i+sx2]; acc3 = acc3 + data[i+sx3]; 2. Call test() again and measure the read 3 throughput(MB/s) /\* Finish any remaining elements \*/ for (; i < length; i++) { acc0 = acc0 + data[i] turn ((acc0 + acc1) + (acc2 + acc3)); mountain/mountair



### **Today**

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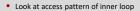


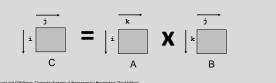
# Miss Rate Analysis for Matrix Multiply

### Assume:

- Block size = 32B (big enough for four doubles)
- Matrix dimension (N) is very large
- Approximate 1/N as 0.0
- Cache is not even big enough to hold multiple rows

### Analysis Method:

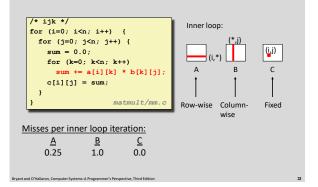




# Layout of C Arrays in Memory (review)

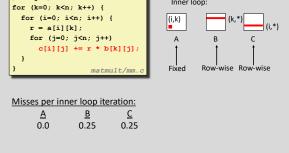
- C arrays allocated in row-major order
- each row in contiguous memory locations
   Stepping through columns in one row:
  - for (i = 0; i < N; i++)</pre>
    - sum += a[0][i];
  - accesses successive elements
  - if block size (B) > sizeof(a<sub>ij</sub>) bytes, exploit spatial locality
     miss rate = sizeof(a<sub>ij</sub>) / B
- Stepping through rows in one column:
  - for (i = 0; i < n; i++)</pre>
  - sum += a[i][0];
  - accesses distant elements
  - no spatial locality!
    - miss rate = 1 (i.e. 100%)

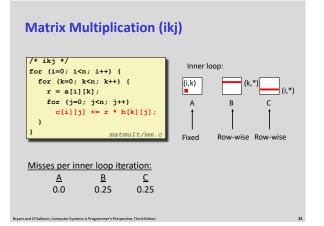
# **Matrix Multiplication (ijk)**

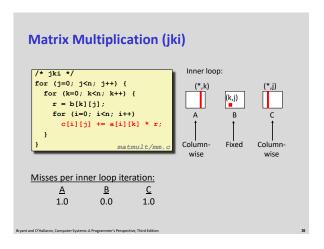


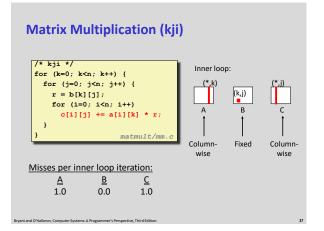
#### **Matrix Multiplication (jik)** /\* jik \*/ Inner loop: for (j=0; j<n; j++) { for (i=0; i<n; i++) {</pre> (\*.i) sum = 0.0; (i,j) (i,\*) for (k=0; k<n; k++)</pre> sum += a[i][k] \* b[k][j]; B A С c[i][j] = sum ł matmult/mm c Row-wise Column Fixed wise Misses per inner loop iteration: B <u>A</u> <u>C</u> 0.25 0.0 1.0

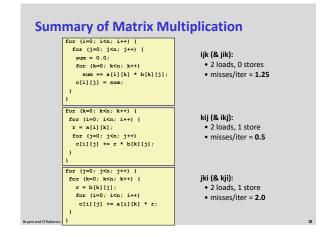
# Matrix Multiplication (kij) /\* kij \*/ for (k=0; k<n; k++) { Inner loop:



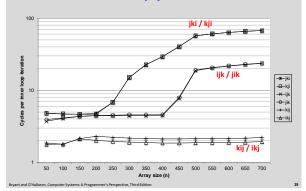








**Core i7 Matrix Multiply Performance** 

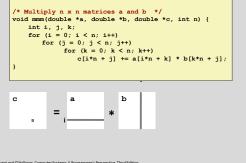


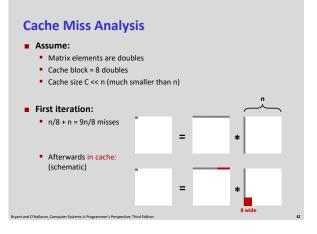
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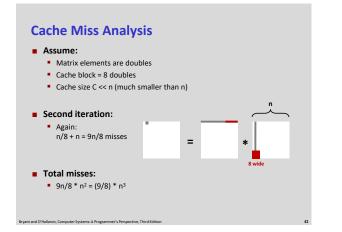
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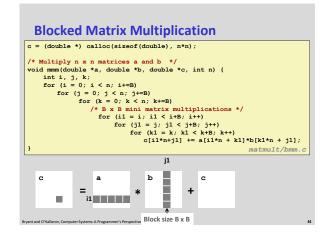
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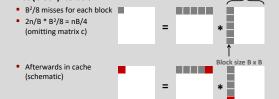


### **Cache Miss Analysis**

### Assume:

- Cache block = 8 doubles
- Cache size C << n (much smaller than n)</li>
- Three blocks I fit into cache: 3B<sup>2</sup> < C

### First (block) iteration:



n/B blocks

# **Cache Miss Analysis**

# Assume:

- Cache block = 8 doubles Cache size C << n (much smaller than n)</li>
- Three blocks I fit into cache: 3B<sup>2</sup> < C

#### n/B blocks Second (block) iteration:

=

Block size B x B

### Same as first iteration

- 2n/B \* B<sup>2</sup>/8 = nB/4
- Total misses:
- nB/4 \* (n/B)<sup>2</sup> = n<sup>3</sup>/(4B)

### **Blocking Summary**

- No blocking: (9/8) \* n<sup>3</sup>
- Blocking: 1/(4B) \* n<sup>3</sup>
- Suggest largest possible block size B, but limit 3B<sup>2</sup> < C!</p>

### Reason for dramatic difference:

- Matrix multiplication has inherent temporal locality: Input data: 3n<sup>2</sup>, computation 2n<sup>3</sup>
- Every array elements used O(n) times!
- But program has to be written properly

# **Cache Summary**

### Cache memories can have significant performance impact

### You can write your programs to exploit this!

- Focus on the inner loops, where bulk of computations and memory accesses occur.
- Try to maximize spatial locality by reading data objects with sequentially with stride 1.
- Try to maximize temporal locality by using a data object as often as possible once it's read from memory.