Cache Memories

CSci 2021: Machine Architecture and Organization April 1st-3rd, 2020

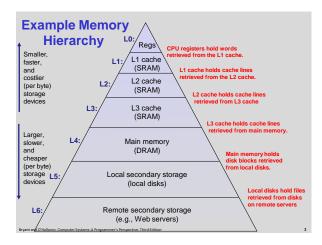
Your instructor: Stephen McCamant

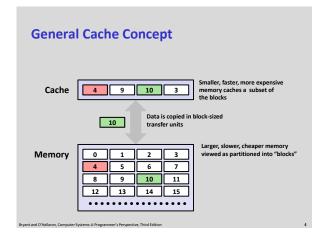
Based on slides originally by: Randy Bryant, Dave O'Hallaron

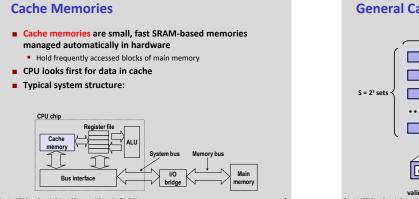
Today

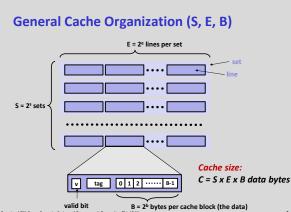
-

- Cache memory organization and operation
 - Performance impact of caches
 - The memory mountain
 - Rearranging loops to improve spatial locality
 - Using blocking to improve temporal locality

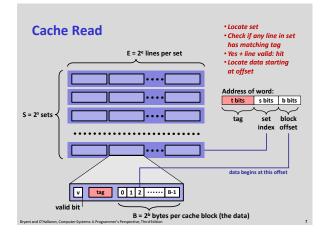


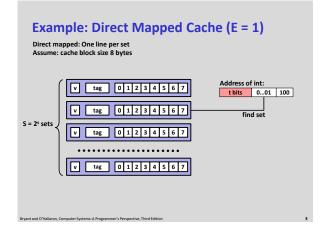






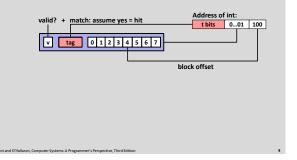
1

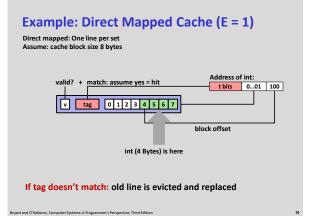


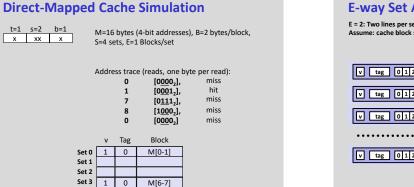


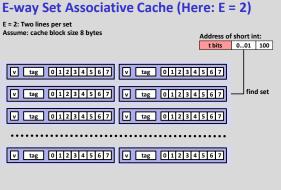
Example: Direct Mapped Cache (E = 1)

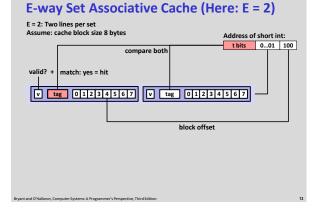
Direct mapped: One line per set Assume: cache block size 8 bytes



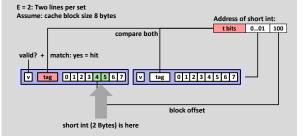






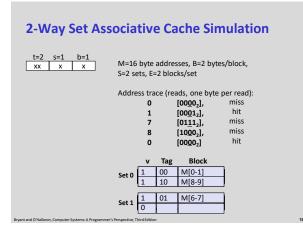


E-way Set Associative Cache (Here: E = 2)



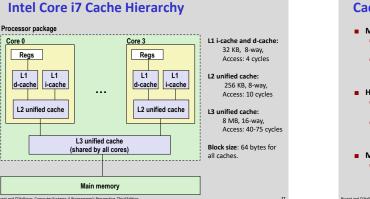
No match:

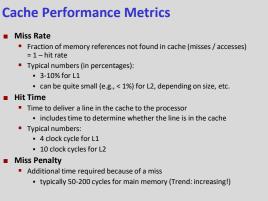
- · One line in set is selected for eviction and replacement
- · Replacement policies: random, least recently used (LRU), ...



Core 0

What about writes? Multiple copies of data exist: L1, L2, L3, Main Memory, Disk What to do on a write-hit? Write-through (write immediately to memory) Write-back (defer write to memory until replacement of line) Need a dirty bit (line different from memory or not) What to do on a write-miss? Write-allocate (load into cache, update line in cache) Good if more writes to the location follow No-write-allocate (writes straight to memory, does not load into cache) Typical Write-through + No-write-allocate Write-back + Write-allocate



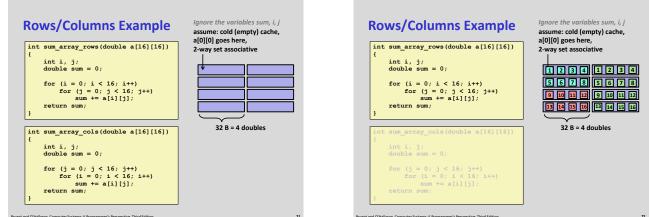


Let's think about those numbers Huge difference between a hit and a miss Could be 100x, if just L1 and main memory Would you believe 99% hits is twice as good as 97%? Consider: cache hit time of 1 cycle miss penalty of 100 cycles Average access time: 97% hits: 1 cycle + 0.03 * 100 cycles = 4 cycles 99% hits: 1 cycle + 0.01 * 100 cycles = 2 cycles This is why "miss rate" is used instead of "hit rate"

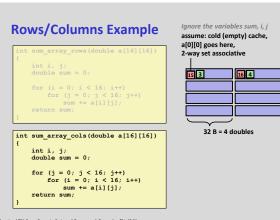
Writing Cache Friendly Code

- Make the common case go fast
- Focus on the inner loops of the core functions
- Minimize the misses in the inner loops
 - Repeated references to variables are good (temporal locality)
 - Stride-1 reference patterns are good (spatial locality)

Key idea: Our qualitative notion of locality is quantified through our understanding of cache memories



ar Surtemr A Pror



15 3	16 4

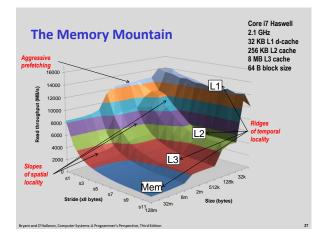
Today

- Cache organization and operation
- Performance impact of caches
 - The memory mountain
 - Rearranging loops to improve spatial locality
 - Using blocking to improve temporal locality

The Memory Mountain

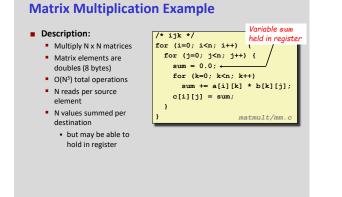
- Read throughput (read bandwidth)
 Number of bytes read from memory per second (MB/s)
- Memory mountain: Measured read throughput as a function of spatial and temporal locality.
 - Compact way to characterize memory system performance.

Memory Mountain Test Function long data[MAXELEMS]; /* Global array to traverse */ /* test - Iterate over first "elems" elements of * array "data" with stride of "stride", using * using 4x4 loop unrolling. Call test() with many combinations of elems and stride. int test(int elems, int stride) { long i, sx2=stride*2, sx3=stride*3, sx4=stride*4; long acc0 = 0, acc2 = 0, acc2 = 0; long length = elems, limit = length - sx4; For each elems and stride: 1. Call test() Combine 4 elements at a time */ once to warm up for (i = 0; i < limit; i += sx4) { the caches. or (i = 0; i < limit; i += sx4) { acc0 = acc0 + data[i]; acc1 = acc1 + data[i+stride]; acc2 = acc2 + data[i+sx2]; acc3 = acc3 + data[i+sx3]; 2. Call test() again and measure the read 3 throughput(MB/s) /* Finish any remaining elements */ for (; i < length; i++) { acc0 = acc0 + data[i] turn ((acc0 + acc1) + (acc2 + acc3)); mountain/mountair



Today

- Cache organization and operation
- Performance impact of caches
 - The memory mountain
 - Rearranging loops to improve spatial locality
 - Using blocking to improve temporal locality

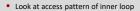


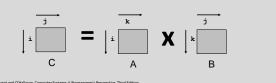
Miss Rate Analysis for Matrix Multiply

Assume:

- Block size = 32B (big enough for four doubles)
- Matrix dimension (N) is very large
- Approximate 1/N as 0.0
- Cache is not even big enough to hold multiple rows

Analysis Method:

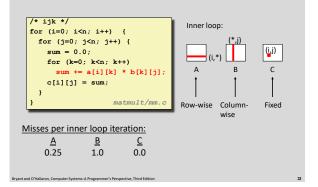




Layout of C Arrays in Memory (review)

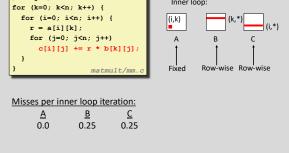
- C arrays allocated in row-major order
- each row in contiguous memory locations
 Stepping through columns in one row:
 - for (i = 0; i < N; i++)</pre>
 - sum += a[0][i];
 - accesses successive elements
 - if block size (B) > sizeof(a_{ij}) bytes, exploit spatial locality
 miss rate = sizeof(a_{ij}) / B
- Stepping through rows in one column:
 - for (i = 0; i < n; i++)</pre>
 - sum += a[i][0];
 - accesses distant elements
 - no spatial locality!
 - miss rate = 1 (i.e. 100%)

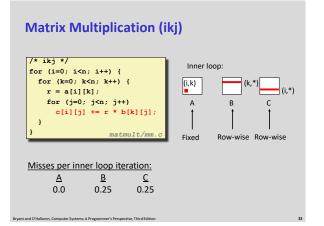
Matrix Multiplication (ijk)

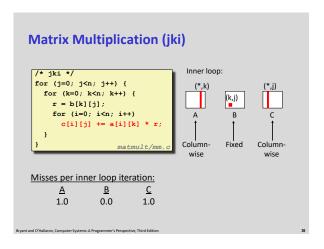


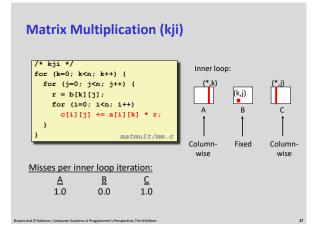
Matrix Multiplication (jik) /* jik */ Inner loop: for (j=0; j<n; j++) { for (i=0; i<n; i++) {</pre> (*.i) sum = 0.0; (i,j) (i,*) for (k=0; k<n; k++)</pre> sum += a[i][k] * b[k][j]; B A С c[i][j] = sum ł matmult/mm c Row-wise Column Fixed wise Misses per inner loop iteration: B <u>A</u> <u>C</u> 0.25 0.0 1.0

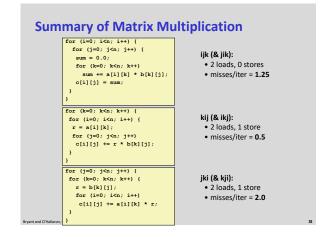
Matrix Multiplication (kij) /* kij */ for (k=0; k<n; k++) { Inner loop:



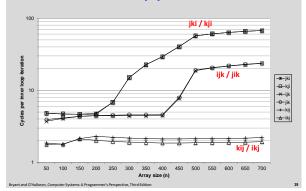








Core i7 Matrix Multiply Performance

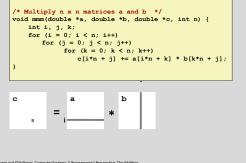


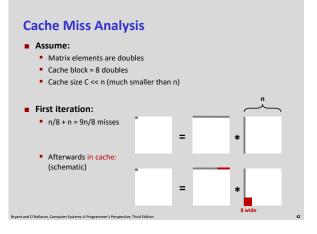
Today

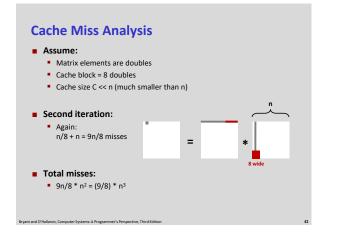
-

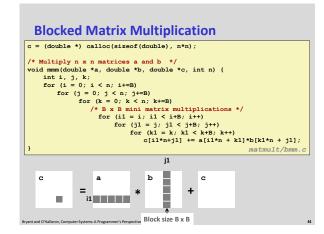
- Cache organization and operation
 - Performance impact of caches
 - The memory mountain
 - Rearranging loops to improve spatial locality
 - Using blocking to improve temporal locality









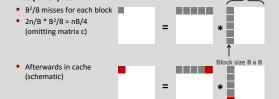


Cache Miss Analysis

Assume:

- Cache block = 8 doubles
- Cache size C << n (much smaller than n)
- Three blocks I fit into cache: 3B² < C

First (block) iteration:



n/B blocks

Cache Miss Analysis

Assume:

- Cache block = 8 doubles Cache size C << n (much smaller than n)
- Three blocks I fit into cache: 3B² < C

n/B blocks Second (block) iteration:

=

Block size B x B

Same as first iteration

- 2n/B * B²/8 = nB/4
- Total misses:
- nB/4 * (n/B)² = n³/(4B)

Blocking Summary

- No blocking: (9/8) * n³
- Blocking: 1/(4B) * n³
- Suggest largest possible block size B, but limit 3B² < C!</p>

Reason for dramatic difference:

- Matrix multiplication has inherent temporal locality: Input data: 3n², computation 2n³
- Every array elements used O(n) times!
- But program has to be written properly

Cache Summary

Cache memories can have significant performance impact

You can write your programs to exploit this!

- Focus on the inner loops, where bulk of computations and memory accesses occur.
- Try to maximize spatial locality by reading data objects with sequentially with stride 1.
- Try to maximize temporal locality by using a data object as often as possible once it's read from memory.