

```

%%function x = backsolv0 (A,b)
% function x =
% Solves an upper triangular system
% by back-substitution.
%-----
n = size(A,1);
x = zeros(n,1);
for i=n:-1:1
    t = b(i);
    for j=i+1:n
        t = t - A(i,j)*x(j) ;    | repeat: (n-i) times
    end                          | 2 ops
    x(i) = t/A(i,i) ;           | 1 op
end

```

operation count:

$$n \sum_{i=1}^{n-1} [2(n-i) + 1]$$

$$\sum_{k=0}^{n-1} [2k + 1] = (n-1)*n + n = n^2 \text{ exactly..}$$

=====

ope. count GE.

```

%%function [x] = gauss (A, b)
% function [x] = gauss (A, b)
% solves A x = b by Gaussian elimination
%-----
n = size(A,1) ;
for k=1:n-1
    for i=k+1:n
        piv = A(i,k) / A(k,k) ;    | repeat (n-k) times:
        A(i,k+1:n+1)=A(i,k+1:n+1)-piv*A(k,k+1:n+1); | 1 op +
    end                          | 2 * (n-k+1)=2(n-k)+2
end
end

```

$$n-1 \sum_{k=1}^{n-1} (n-k)(2(n-k)+3)$$

set j = n-k

$$n-1 \sum_{j=1}^{n-1} j(2j+3)$$

$$n-1 \sum_{j=1}^{n-1} [2j^2 + 3j]$$

$$2 \sum_{j=1}^{n-1} j^2 + 3 \sum_{j=1}^{n-1} j = 2(n-1)n(2n-1)/6 + 3n(n-1)/2$$

$$= n(n-1) [(2n-1)/3 + 3/2]$$

$$= n(n-1) (2n/3 + 7/6)$$

$$\approx \overset{\text{=====}}{2 n^3/3 + 0(n^2)} \quad 0(n^3)$$

Recall: $\sum_{j=1}^n j^2 = n(n+1)(2n+1)/6$