

$$s_1 = fl(x_1 y_1) = x_1 y_1(1+\eta_1)$$

$$s_2 = fl(s_1 + fl(x_2 y_2))$$

$$= [x_1 y_1(1+\eta_1) + x_2 y_2 (1+\eta_2) ] (1+\varepsilon_2)$$

$$s_3 = fl(s_2 + fl(x_3 y_3)) = [s_2 + x_3 y_3(1+\eta_3)](1+\varepsilon_3)$$

$$= [[x_1 y_1(1+\eta_1) + x_2 y_2 (1+\eta_2) ] (1+\varepsilon_2) + x_3 y_3(1+\eta_3) ](1+\varepsilon_3)$$

$$x_1 y_1 (1+\eta_1)(1+\varepsilon_2)(1+\varepsilon_3) +$$

$$x_2 y_2 (1+\eta_2)(1+\varepsilon_2)(1+\varepsilon_3) +$$

$$x_3 y_3 (1+\eta_3) ](1+\varepsilon_3)$$

for  $s_n$ :

$$s_n = \sum_{i=1}^n x_i y_i (1+\eta_i) \prod_{j=i}^n (1+\varepsilon_j)$$