## A QUICK INTRODUCTION TO MATLAB

- Very brief intro to matlab -
- Basic operations and a few illustrations
$>$ This set is independent from rest of the class notes.
> Matlab will be covered in recitations and occasionally in class


## Intro to matlab - getting started



To start type 'matlab' under a unix terminal (or click icon under windows). You will get a matlab GUI with a command window that has the prompt: >>.
> I prefer to use matlab without the GUI [especially for the demos given in class]. In linux or mac OS this is done by typing into a terminal the command
\% matlab -nodesktop
instead of
\% matlab
$>$ To exit matlab use exit or quit
>> quit

## Getting Help

> Most of the help for matlab is online. In the GUI you can click on the '?' icon.
$>$ Often it is faster to get help by typing into the matlab window
>> help topic
$>$ Examples
>> help or $\quad \gg$ help ref or $\gg$ help punct
$>$ Alternatively you can get the same info in a pop-out window by typing:
>> doc topic

## For example: >> doc diary gave this:


> '>> help' or '>> doc' by itself will list the help topics
> Same thing as clicking the '?' icon in the GUI.

## Example:

```
>> help mod
mod modulus (signed remainder after division).
    ... followed by a few lines of explanation...
    ... then: shows related function (s):
    See also REM.
>> a = 25; b = 3;
>> mod(a,b)
ans =
>> mod(a,5)
ans =
        0
>> mod(25.2,2)
ans =
    1.2000
```


## Basic Operations in Matlab

$>$ The following is on the basics of matlab. It starts with some basic operations and the help command.
$>$ A useful command I used to generate some of these examples is >>diary filename.
$>$ This is equivalent to a typescript. Everything displayed on screen is saved in a file. [useful for homeworks]
$>$ In what follows: Everything that starts with >> is what I typed into the matlab prompt.

## Simple operations

```
>> 4+6+3
ans =
    1 3
>> 4*20+ 3*57 + exp(-0.1)
ans =
    251.9048
```

> |This is what I typed in |These lines are matlab's |answer
|This is what I typed in |These lines are matlab's |answer

Note: ending versus not ending command with semi-colon.

| >> a +2 | <----- do command + display result |
| :--- | :--- |
| ans $=$ | <---- results of operation shown |
| 25 |  |
| >> a+2; | <---- do command - do not display result |
| >> | <---- result not displayed |

## Squaring and powers:

>> $a^{\wedge}=12 ;$
>

```
ans =
    144
>> a^4
ans =
    20736
```

```
Right/Left divide (/ and \\)
>> \(\mathrm{a}=12 ; \mathrm{b}=3\);
>> a/b
ans \({ }_{4}\)
>> \(a \backslash b\)
ans \({ }_{0}^{=} .2500\)
>> b/a
ans =
    0.2500
```

> Important because these have their equivalent versions for matrices

```
more, disp, format
```

```
>> more on
```

> more on allows you to scroll page by page
$>$ disp(x) simply displays x without fillers

## format selects format for displaying results :

Options: format short, long, rat, ...
>> format short
>> pi
ans $=$
3.1416

```
>> format long
>> pi
ans =
    3.141592653589793
>> format rat
>> pi
ans = 355/113
```

> Also useful: format compact [avoids empty line feeds.. useful for homeworks]
$>$ The command '>> who' lists the variable currently stored >> who
your variables are:
a ans b
>>
$>$ See also: '>> whos' which has more detail
> Earlier we invoked exp which is the exponential function.
> Get info by typing
>> help exp
exp exponential. | answer:
$\exp (\mathrm{x})$ is the exponential of the elements of x , e to the $x$. for complex $z=x+i * y$, $\exp (z)=\ldots$. + a few more lines of explanation ending with
see also $\log , \log 10$, expm, expint.
overloaded methods
help sym/exp.m
( Explore the other elementary functions:
>> help elfun
will list all the elementary functions used by matlab - A long list that starts like this :
elementary math functions. trigonometric.

| $\sin$ | - sine. |
| :--- | :--- |
| sinh | hyperbolic sine. |
| asin | - inverse sine. |
| asinh | - inverse hyperbolic sine. |
| $\cos$ | - cosine. |

## Complex Numbers

```
>> c = 1 - 2i
c = 1.0000-2.0000i
>> conj(c)
ans =
    1.0000 + 2.0000i
>> c*conj(c)
ans =
>> abs(c)
ans
    2.2361
```

$>$ Note: $\operatorname{abs}(\mathrm{c})$ is the modulus of c

## Matrices

> To define a matrix enter entries row by row, separated by a ";"

$$
>A=\left[\begin{array}{lllllllllll}
1 & 1 & 1 & ; & 2 & 2 & 2 & ; & 3 & 3 & 3
\end{array}\right]
$$

$$
\begin{array}{lll}
A= & & \\
1 & 1 & 1 \\
2 & 2 & 2 \\
3 & 3 & 3
\end{array}
$$

> Could use commas for separating columns (not required):
$\gg A=[1,1,1 ; 2,2,2 ; 3,3,3]$;
> So: ',' separates columns and ';' separates rows. The above matrix can also be defined as
$\gg A=[[1 ; 2 ; 3],[1 ; 2 ; 3],[1 ; 2 ; 3]]$
> Can use matrices as blocks [very convenient!]
$\gg B=[A, A]$
$B=$

| 1 | 1 | 1 | 1 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 2 | 2 | 2 | 2 | 2 |
| 3 | 3 | 3 | 3 | 3 | 3 |

« Show the result of the command: $\gg C=\left[A,-A ; A^{*} A, 2^{*} A\right]$
> Two important special matrix functions
eye(n) and zero(n)
>> A = eye(5)
|Identity matrix of size 5
$\mathrm{A}=$

| 1 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 0 | 1 |

> It is enough to say eye (5) in this example but ...
$>$ 'eye' is defined for rectangular matrices too

| $\gg A=\operatorname{eye}(6,3)$ |  |  |
| :--- | :--- | :--- |
| $A=$ |  |  |
| 1 | 0 | 0 |
| 0 | 1 | 0 |
| 0 | 0 | 1 |
| 0 | 0 | 0 |
| 0 | 0 | 0 |
| 0 | 0 | 0 |

$>\operatorname{zeros}(m)$ or $\operatorname{zeros}(m, n)$ is defined similarly:

| P> | $A$ | $=$ | $z e r o s$ |
| :--- | :--- | :--- | :--- |
|  | $(3,4)$ |  |  |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
|  | 0 | 0 | 0 |

## Defining a vector through loop constructs

```
>> start=0; inc=2; last=12;
>> start:inc:last
ans \begin{tabular}{lllllll} 
\\
0 & 2 & 4 & 6 & 8 & 10 & 12
\end{tabular}
>> 0:2:12
ans =
    0
2
4
\(6 \quad 8 \quad 10\)12
```

> Can also use real numbers

```
start = 0.0; inc = 0.15; last = 1.0;
```

>> start:inc:last

```
ans =
    0
2-20
>> \(\mathrm{x}=0: 0.15: 1\)
\(\mathrm{x}=\begin{array}{lllllll}0 & 0.1500 & 0.3000 & 0.4500 & 0.6000 & 0.7500 & 0.9000\end{array}\)
\(>\) Quite convenient for doing simple plots (see later)
> Can use loop constructs in matrices as well:
\(\left.\gg A=[1: 4 ; 4: 7] \quad \left\lvert\, \begin{array}{l}\text { 1st row }=1: 4=1 \\ \text { 2nd row }=4: 7=4\end{array}\right.\right)\)
\(A=\begin{array}{llll} & & & \\ & 2 & 3 & 4 \\ 4 & 5 & 6 & 7\end{array}\)
>> \(A=[0.0: 0.1: 0.5 ; 2.1: 0.2: 3.1] \mid\) Must have same number of entries in the 2 rows
\(\mathrm{A}=\)
\(\begin{array}{rlllll}0 & 0.1000 & 0.2000 & 0.3000 & 0.4000 & 0.5000 \\ 2.1000 & 2.3000 & 2.5000 & 2.7000 & 2.9000 & 3.1000\end{array}\)

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\section*{The function 'size'}

Everything in matlab is considered a matrix. size(x) gives the dimensions of the object x
```

$\gg x=x=0.0: 0.1: 0.8 ; \quad \mid 0.00 .1 \ldots 0.8$ ( 9 entries)
>> size(x)
ans $\begin{gathered}= \\ 1\end{gathered}$
<---- 1 row, 9 columns
$\gg A=[1: 4 ; 4: 7] ;$
>> size(A)
ans $\begin{gathered}= \\ 2\end{gathered}$
<---- 2 rows 4 columns
>> size(pi)
ans =
$1 \quad 1$
| number pi = a scalar
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## Vector operations

```
>> x+y; | adding 2 vectors of same shape
>> 0.15*x -.0*y; | linear comb. of x and y
>> y = exp(-x) | point-wise exponential of -x
y = 1.0000 0.8607
0.7408
0.6376
0.5488 0.4724
\(>\) cannot square a vector:
>>
\[
\gg\left[\begin{array}{lll}
1 & 2 & 3
\end{array}\right] \sim 2
\]
Error using
Inputs must be a scalar and a square matrix.
To compute elementwise POWER, use POWER (.^) instead.

\section*{Pointwise (array) product:}
\[
\begin{aligned}
& \gg a=[2,34] ; b=\left[\begin{array}{lll}
0 & 5 & 6
\end{array}\right] ; \\
& \gg c=a \cdot * b \\
& c=01524
\end{aligned}
\]

Let us go back to \(z=x^{2}\). To square the components of \(\boldsymbol{x}\), do:
>> \(\mathrm{y}=\mathrm{x}\).^2
or
>> \(\mathrm{y}=\mathrm{x}\).* x
\(y=\begin{array}{lllllll}0 & 0.0225 & 0.0900 & 0.2025 & 0.3600 & 0.5625 & 0.8100\end{array}\)
2-24

\section*{Simple plotting}
> Matlab provides powerful graphics capabilities - 2D plots, 3D surfaces.
> The simplest command: >> plot \((\mathrm{x}, \mathrm{y})\) causes matlab to popout a window which has the following plot

* Try the following commands and explain what they do
\[
\begin{aligned}
& x=[0: 0.01: 2 * p i] ; \\
& y=x . * \cos (x) ; \\
& \text { plot }(x, y) ; \\
& \text { hold on } \\
& z=1 . /(1 / 6+y \cdot \wedge 2) ; \\
& \text { plot }(x, z, r--\prime) ; \\
& \text { plot }([0,2 * p i],[00]) ; \\
& \text { plot }([0,0],[0,7]) ; \\
& \text { axis }([-17-48])
\end{aligned}
\]

\section*{Basic operators}
\(>\) Standard arithmetic operators:
\[
+,-, *, /
\]
\(>\) Unary operations (for example \(-\boldsymbol{A}\) ).
> Back-slash operator:
\[
x=A \backslash b
\]
where \(\boldsymbol{A}\) is a matrix and \(\boldsymbol{b}\) a vector (or matrix) then \(\boldsymbol{x}=\boldsymbol{A}^{-1} \boldsymbol{b}\). [to be seen later in the class.]
\begin{tabular}{|c|c|c|}
\hline \multirow{6}{*}{- Relational operators.} & - Equal & \(=\) \\
\hline & - Not equal & \(\sim\) \\
\hline & - Less than & < \\
\hline & - Greater than & \(>\) \\
\hline & - Less than or equal & \(<=\) \\
\hline & - Greater than or equal & \(>=\) \\
\hline
\end{tabular}

\section*{Example:}
```

>> a = 1; b = 0; c = 2;
>>a+b+c== c+a+b
ans =
1

```
\(>\) Not to confuse with ' \(=\) ' :
>> \(\mathrm{a}+\mathrm{b}+\mathrm{c}=\mathrm{c}+\mathrm{a}+\mathrm{b}\)
??? Error: Assignment statements cannot produce a result.
\(>\) Comparisons can be done on vectors and matrices:
\[
\begin{align*}
& \text { >> a = 1:2:20 } \\
& \begin{array}{llllllllll} 
\\
= & 3 & 5 & 7 & 9 & 11 & 13 & 15 & 17 & 19
\end{array} \\
& \text { >> b = 2:2:21 } \\
& \text { b }= \\
& \begin{array}{lllllllll}
2 & 4 & 6 & 8 & 10 & 12 & 14 & 16 & 18
\end{array} \\
& \text { >> } \mathrm{a}==\mathrm{b} \\
& \mathrm{ans}_{0}= \\
& \text { >> } \mathrm{a}+1 \text { == b } \\
& \mathrm{ans}_{1}=1 \\
& 1 \\
& 1 \quad 1 \quad 1 \quad 1 \\
& 1
\end{align*}
\]

Note: 1 means "true", 0 means "false"

\section*{Conditionals}

\section*{If statement}
> Simplest form:
```

if (logical-expression)
commands
end

```
if (logical-expression)
    commands
    elseif (logical-expression)
        commands
    else
        commands
end

\section*{Loops}

\section*{For loop}
> Simplest form:
\[
\begin{aligned}
& \text { for } \mathrm{j}=1 \text { :m } \\
& \quad: \\
& \quad \text { commands } \\
& \quad: \\
& \text { end }
\end{aligned}
\]

Examples of other constructs
for \(j=0: 3: 31\) for \(j=100:-1: 0\) for \(j=0.1: 0.1: 2.4\)

\section*{Example:}

Simple version of script to compute the square root of 5. [shown in class]
```

tol = 1.e-10;
a = 5;
x = a;
for i=1:100
x = 0.5*(x+a/x);
if abs(x^2-a) < tol
break;
end
end

```

\section*{While loop}
> Generic form:

\section*{while (logical) commands \\ end}

For the square example you can achieve the same result with a while loop
```

tol = 1.e-10;
a = 5;
x = a;
while abs(x^2 - a) > tol
x = 0.5*(x+a/x);
end

```
* The above needs a fix [potential for infinite loop]```

